

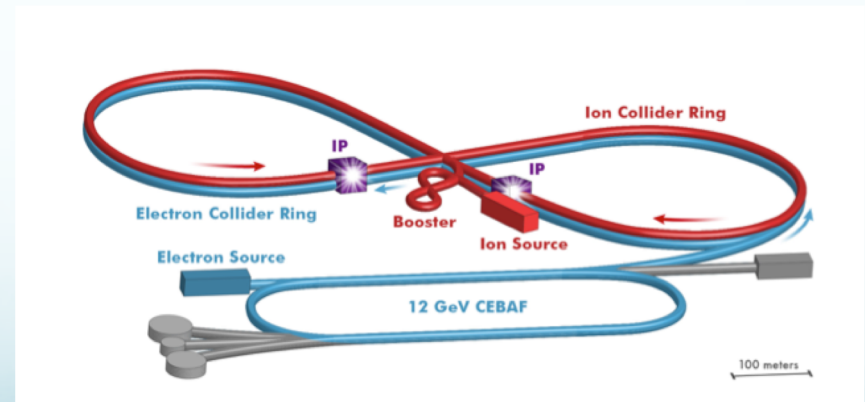
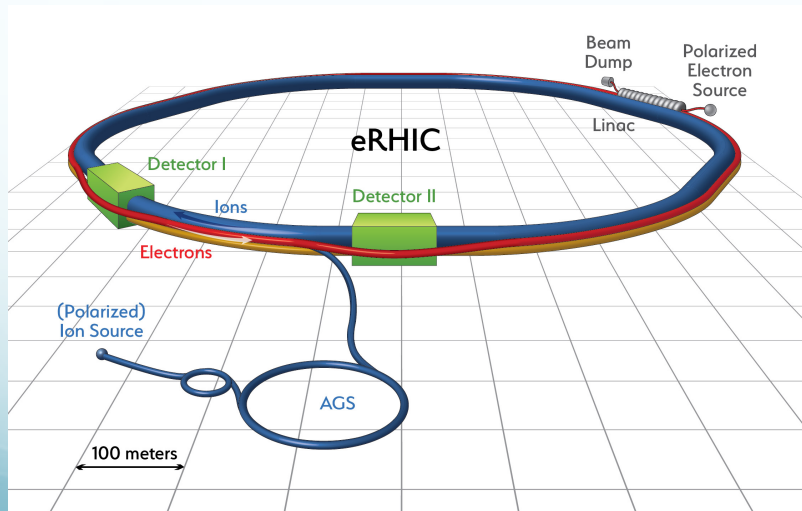
# Review: jets in ep/eA DIS

Zhongbo Kang  
UCLA

2018 Workshop on Probing Quark-Gluon Matter with Jets  
July 23 – 25, 2018

# Jets and EIC

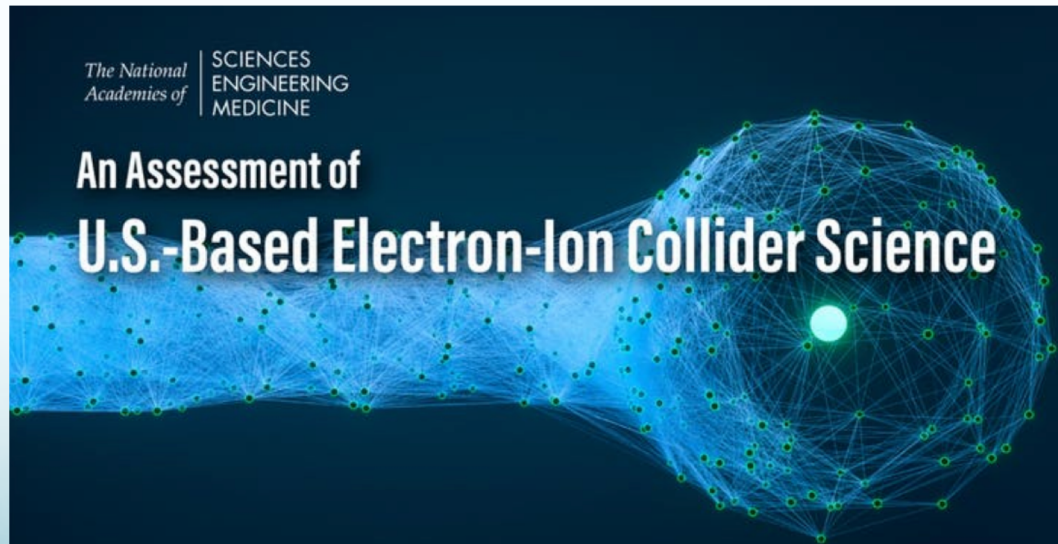
- Goal: discuss possible applications of jet physics to both  $e+p$  and  $e+A$  collisions
  - Consistent with the theme of the workshop, one should discuss the novel tools and observables that are being developed to probe the **cold** quark-gluon matter with jets in electron-ion collisions
- Electron Ion Collider
  - Highest priority for new construction in NSAC 2015 long range plan





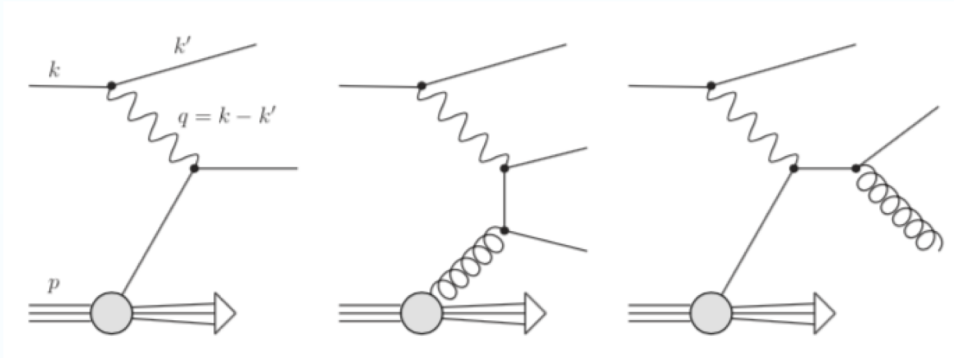
# Jets and EIC

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- Electron Ion Collider
  - Highest priority for new construction in NSAC 2015 long range plan
  - National Academy: report on EIC to be released on July 24

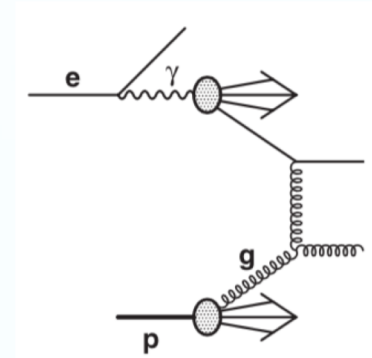


# Jets in DIS

- Deep Inelastic Scattering (DIS) and photon-production



direct:  $Q^2$  large



resolved:  $Q^2 \sim 0$

- Well established QCD factorization formalism

- Usual DIS process with virtual photon  $Q^2$  large

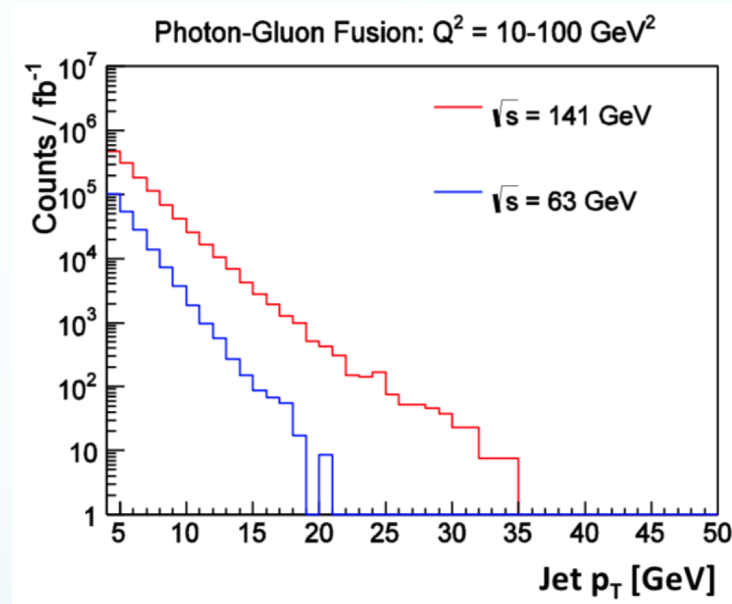
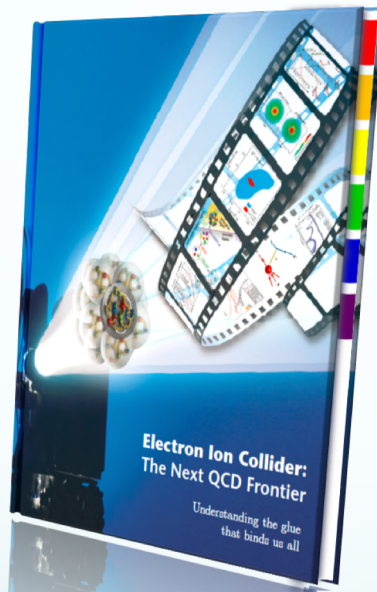
$$d\sigma_{ep \rightarrow e + \text{jets} + X} = \sum_a \int_0^1 d\hat{\sigma}_{ea \rightarrow cd}(x, \alpha_s(\mu_R), \mu_F, \mu_R) f_{a/P}(x, \mu_F) dx,$$

- Photon-production

$$d\sigma_{ep \rightarrow e + \text{jets} + X} = \sum_{a,b} \int_0^1 dx_\gamma \int_0^1 dx_p \underbrace{f_{\gamma/e} f_{b/\gamma}(x_\gamma, \mu_{F\gamma})}_{\text{circled in red}} f_{a/p}(x_p, \mu_{Fp}) d\hat{\sigma}_{ab \rightarrow cd}(x_\gamma, x_p, \alpha_s(\mu_R), \mu_{F\gamma}, \mu_{Fp}, \mu_R),$$

# Jets at an EIC

- It was realized only **recently** that jet measurements are possible at EIC
  - EIC white paper does not contain study on jet physics: arXiv:1212.1701 (recently updated on Nov. 30, 2014)



Brian Page, Santa Fe Jets and Heavy Flavor Workshop 2016

- Our outstanding experimental colleagues and EIC team made the initial feasibility studies in **e+p** collisions
- No (published) jet studies in **e+A** collisions yet: *EIC would be the very first one*

# Purposes of jet/QCD studies in DIS

- I: Studying QCD/jets to probe
  - Fundamental parameters of QCD: strong coupling constant
  - Parton structure of proton
  - Signature for BSM physics

NNLO + resummation

## LHC THEORY — TOWARDS 1% PRECISION?

*Gavin P. Salam, CERN*

*Joint CTEQ Meeting and 7th International Conference  
on Physics Opportunities at an EIC (POETIC 7)*

- II: Studying QCD/jets to probe QCD medium
  - Cold nuclear matter in e+A collisions
  - Hot quark-gluon plasma in A+A collisions

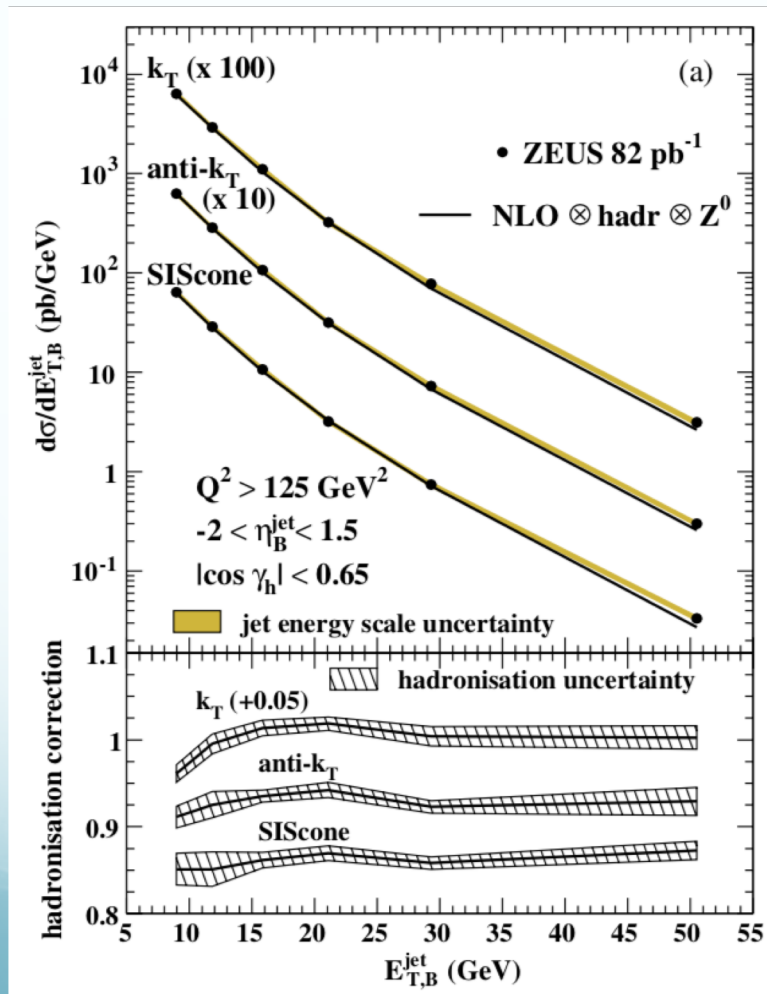
NLO + resummation is probably sufficient at the moment

First e+A jet measurements are still yet to come at EIC

Too many effects need to be taken into account in A+A

# Jets in e+p collisions at HERA

- Jet measurements in e+p collisions are only from HERA
  - Theoretical computations could be obtained through NLOJet++ (Zoltan Nagy, based on Catani-Seymour dipole subtraction method)



REVIEWS OF MODERN PHYSICS, VOLUME 86, JULY-SEPTEMBER 2014

## The hadronic final state at HERA

Paul R. Newman<sup>\*</sup>

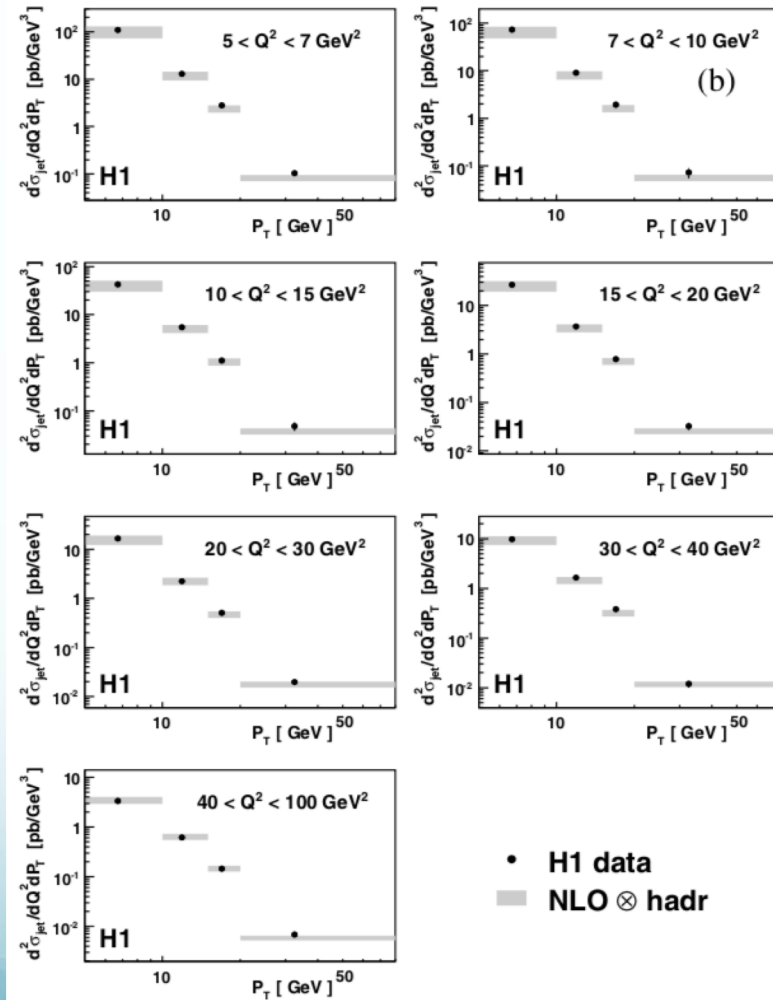
*School of Physics and Astronomy, University of Birmingham,  
Birmingham B15 2TT, United Kingdom*

Matthew Wing<sup>†</sup>

*Department of Physics and Astronomy, University College London,  
Gower Street, London WC1E 6BT, United Kingdom  
and DESY, Notkestrasse 85, 22607 Hamburg, Germany*

# Jets in e+p collisions at HERA

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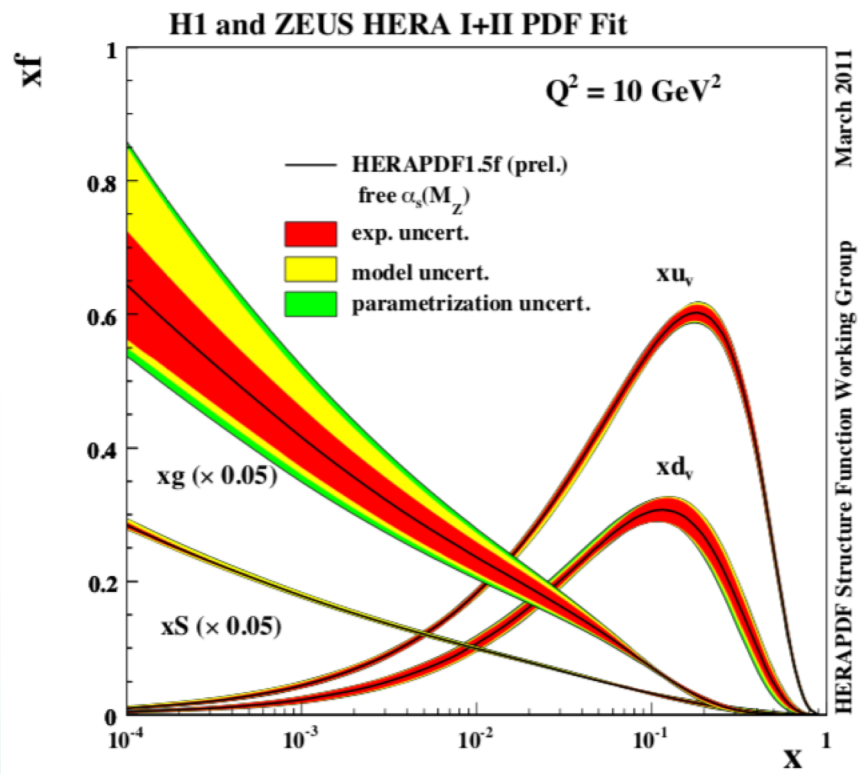
# Jets in e+p collisions

- Jets at HERA are extremely important
  - Constraining the gluon PDF

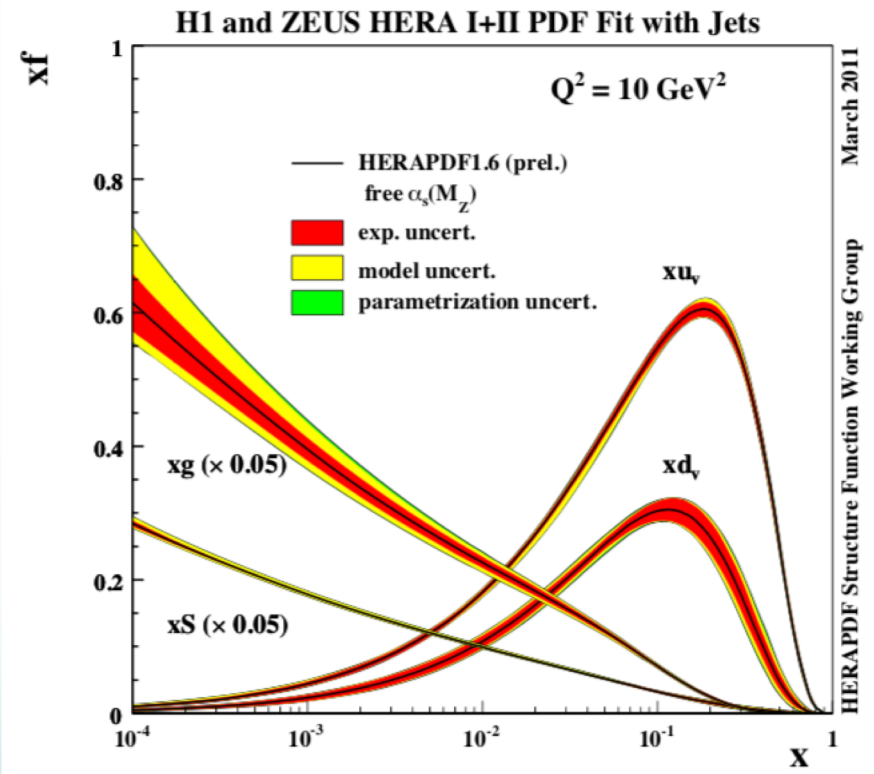
Nuclear Physics B (Proc. Suppl.) 222–224 (2012) January–March 2012

**HERA 2011**

Proceedings of the Ringberg Workshop  
New Trends in HERA Physics 2011



Without jets



With jets

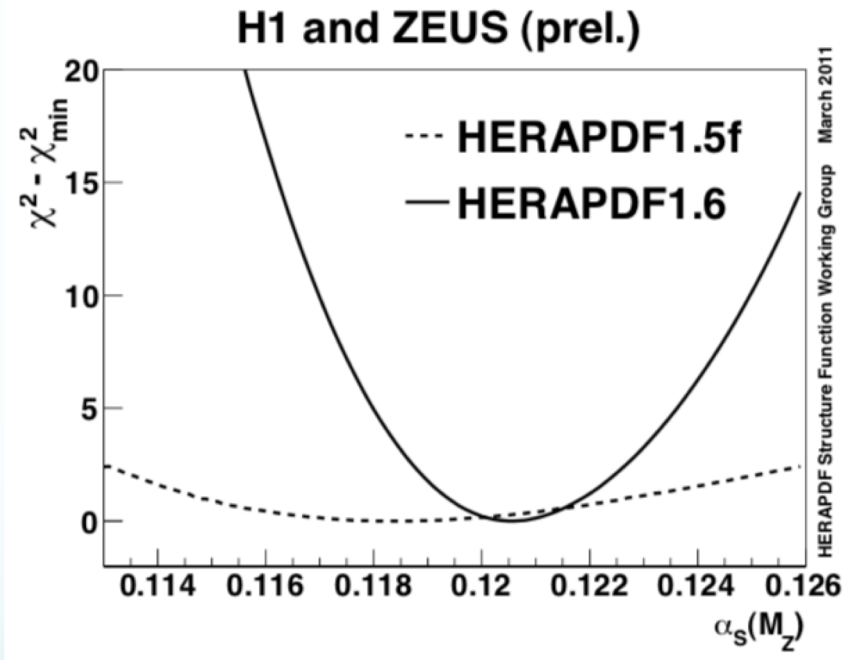
# Jets in e+p collisions

- Jets at HERA are extremely important
  - Constraining the gluon PDFs
  - Determine the strong coupling constant

Nuclear Physics B (Proc. Suppl.) 222–224 (2012) January–March 2012

## HERA 2011

Proceedings of the Ringberg Workshop  
New Trends in HERA Physics 2011

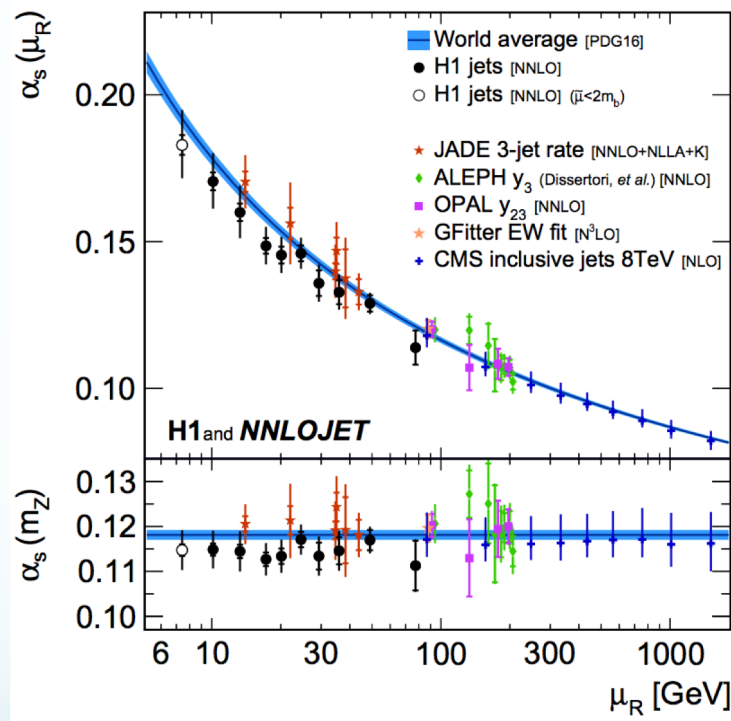


Dashed: without jets  
Solid: with jets



# New developments since then

- NNLO have become available
  - arXiv:1607.04921, Abelof, Boughezal, Liu, Petriello
  - arXiv:1703.05977, Currie, Gehrmann, Huss, Niehues



arXiv: 1709.07251, see more at R. Zlebcik's talk

# Other development: QCD factorization

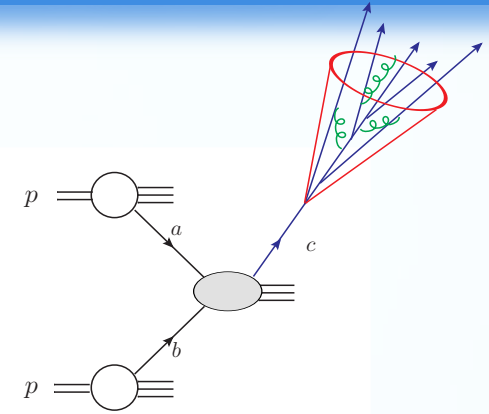
- Single inclusive jet production:  $p + p \rightarrow \text{jet} + X$

$$\frac{d\sigma^{pp \rightarrow \text{jet} X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab}$$

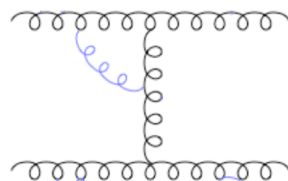


partonic hard-scattering cross section

$$H_{ab} = \alpha_s^2 \left( H_{ab}^{(0)} + \alpha_s H_{ab}^{(1)} + \alpha_s^2 H_{ab}^{(2)} + \dots \right)$$

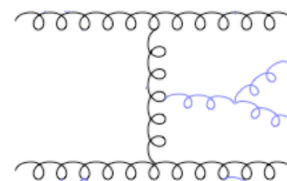


- The idea is simple: dynamics which happen in very different scales do not interfere with each other:  $\Lambda_{\text{QCD}}$  vs  $P_T$



NLO 1990

Ellis, Kunszt, Soper '90

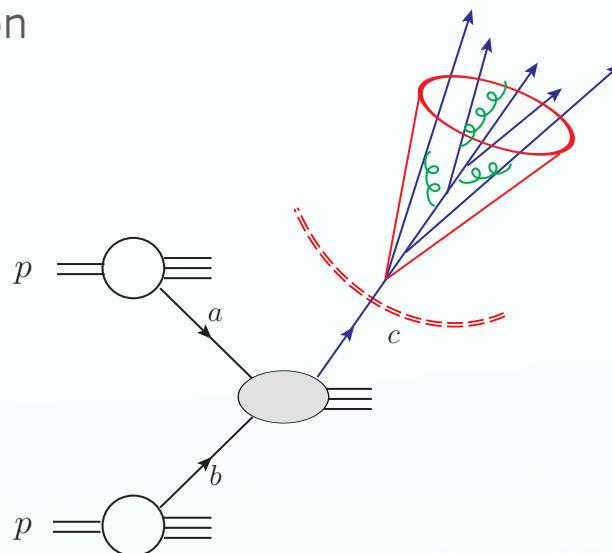


NNLO 2016 ...

Currie, Glover, Pires '16

# Refactorization: semi-inclusive jet function

- When  $R \ll 1$ , the relevant scales for single jet production
  - Two momenta: (1) hard collision:  $p_T$  (2) jet radius can build one:  $p_T R$
  - A further factorization



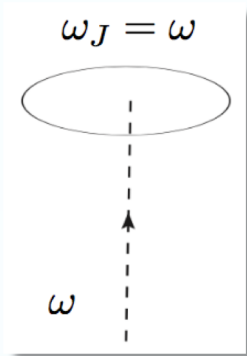
$$\frac{d\sigma^{pp \rightarrow \text{jet } X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes J_c(z, \mu \sim p_T R)$$

- Good thing: semi-inclusive jet function  $J_{q,g}(z, R)$  are purely perturbative

Kang, Ringer, Vitev, arXiv:1606.06732, Dai, Kim, Leibovich, 1606.07411,  
see also, Kaufmann, Mukherjee, Vogelsang, 1506.01415

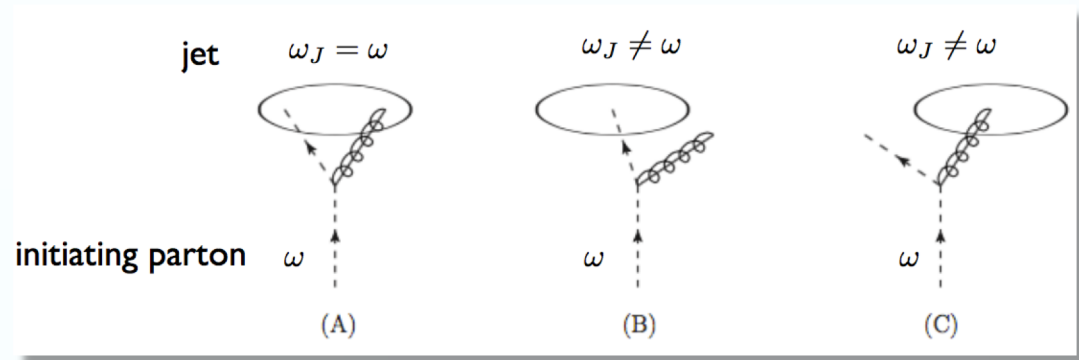
# Semi-inclusive jet functions

- Describe how a parton (q or g) is transformed into a jet (with a jet radius R) and energy fraction z



**LO**

$$J_q^{(0)}(z, \omega_J) = \delta(1 - z)$$



**NLO**

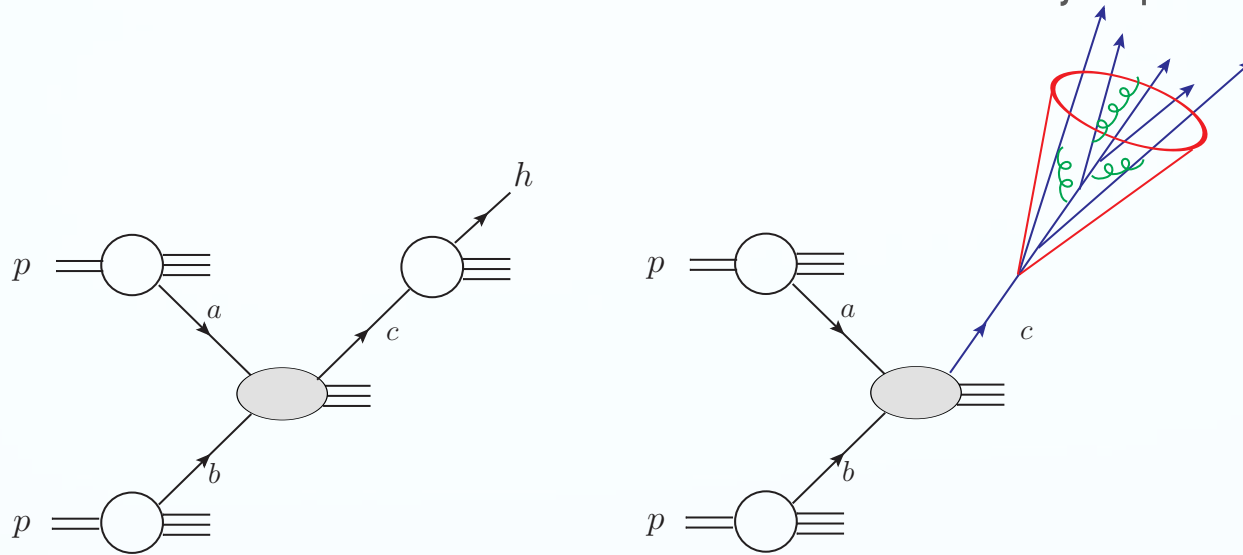
$$z = \omega_J / \omega$$

- Semi-inclusive quark/gluon jet functions follow DGLAP evolution equation, just like hadron fragmentation function

$$\mu \frac{d}{d\mu} J_i(z, \omega_J, \mu) = \frac{\alpha_s(\mu)}{\pi} \sum_j \int_z^1 \frac{dz'}{z'} P_{ji} \left( \frac{z}{z'}, \mu \right) J_j(z', \omega_J, \mu)$$

# Features: unified formalism

- Unified factorization formalism for hadron and jet production

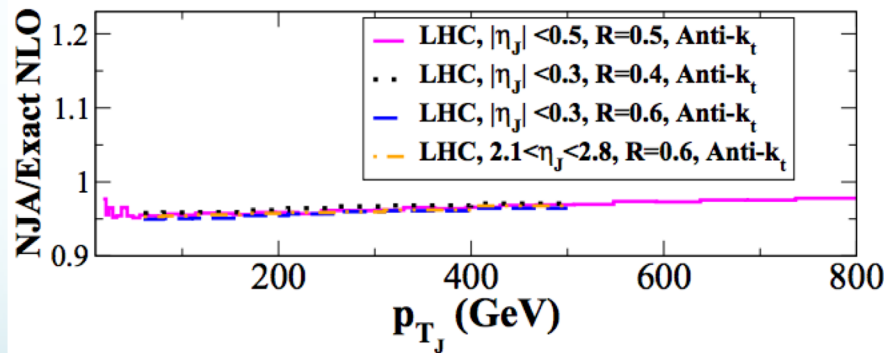
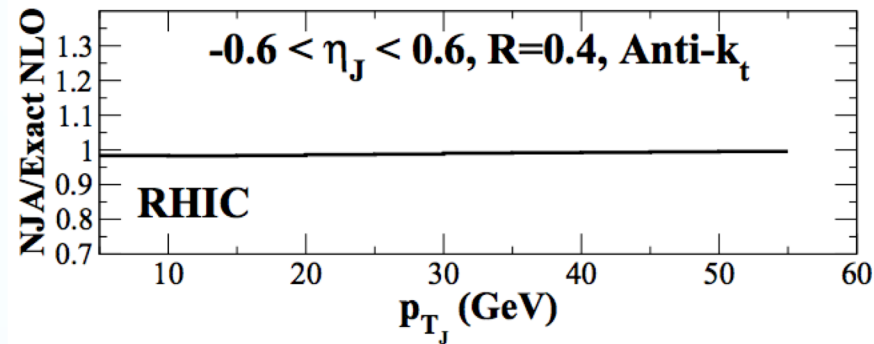


$$\frac{d\sigma^{pp \rightarrow hX}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes D_c^h(z, \mu)$$

$$\frac{d\sigma^{pp \rightarrow \text{jet}X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes J_c(z, \mu \sim p_T R)$$

# Small R is a good approximation

- Even though derived for small R,  $R = 0.7$ , the difference between small R approximation and full result is less than 5%



Mukherjee, Vogelsang, arXiv: 1209.1785

# Ln(R) resummation

- Natural scale for jet functions:  $p_T^* R$

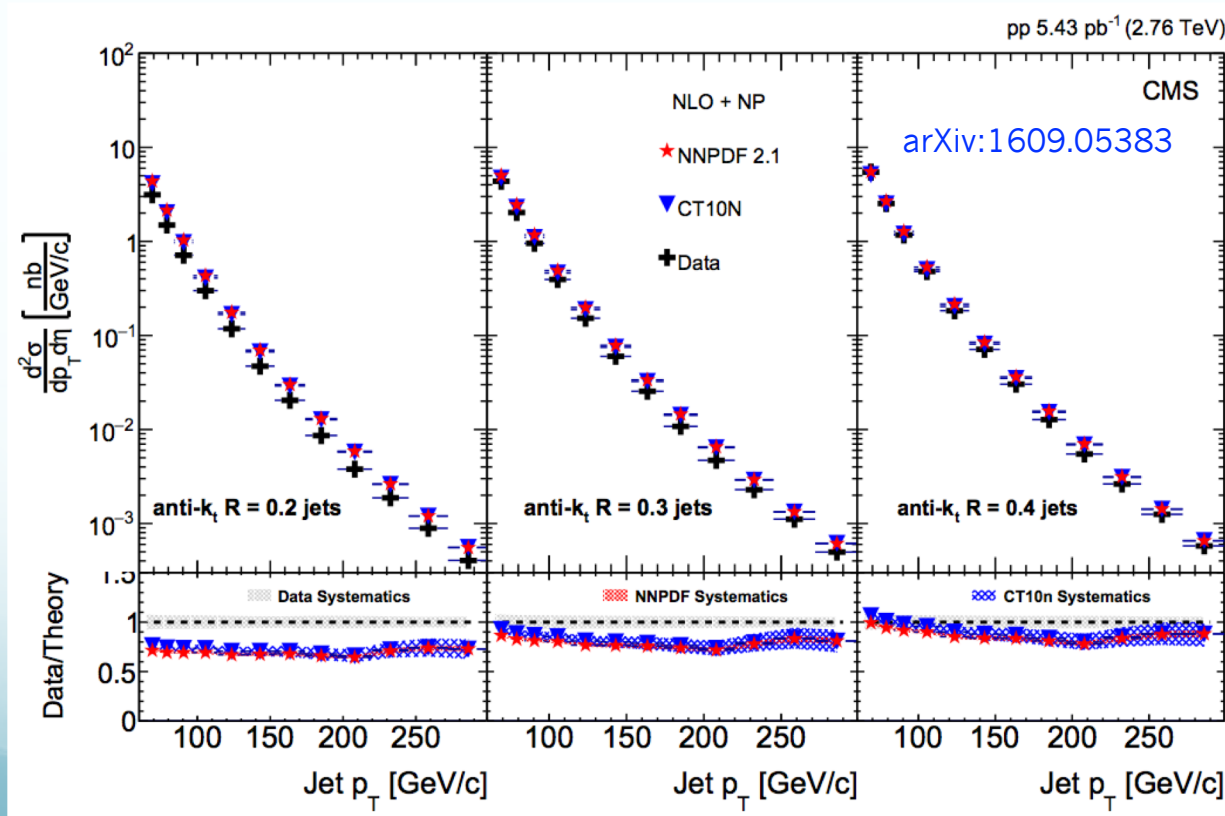
- Jet radius resummation:  $(\alpha_s \ln R)^n$

- Note:  $\ln(R) < 0$  when  $R < 1$



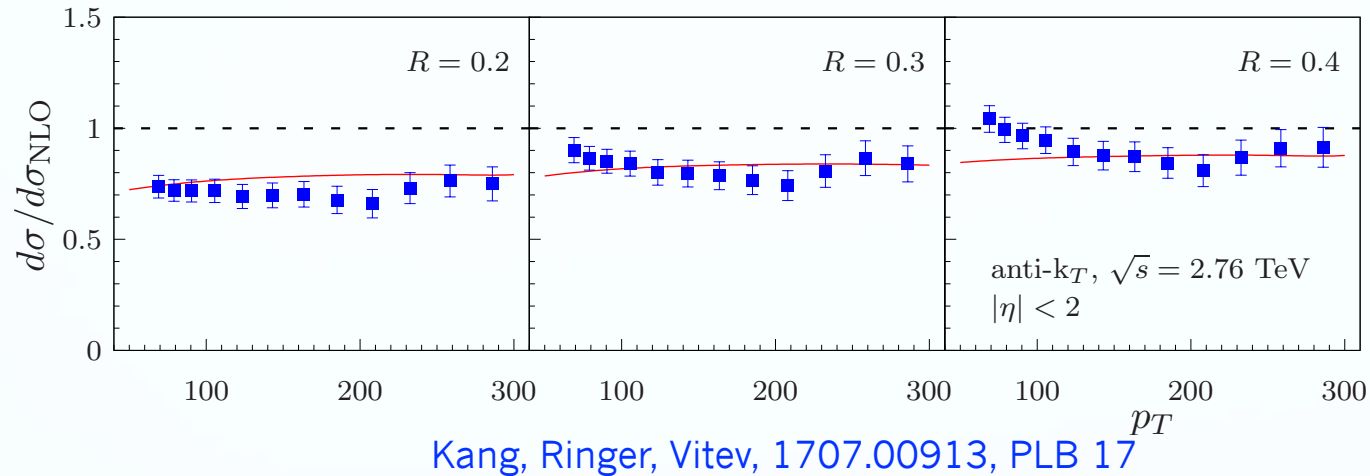
Kang, Ringer, Vitev, arXiv:1606.06732

- Solve experimental puzzle at LHC

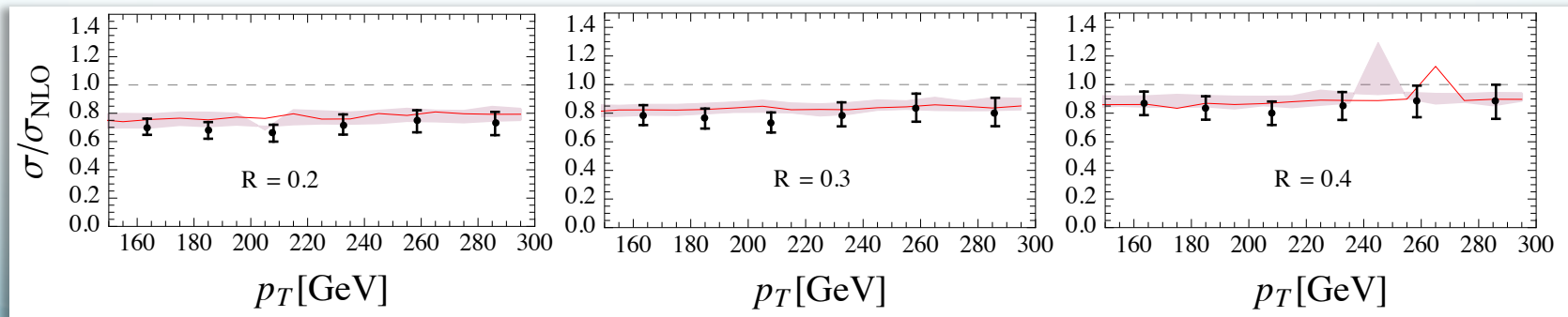


# Effect of $\ln(R)$ resummation

- The  $\ln(R)$  is a big source for the discrepancy



- Threshold resummation further improve the agreement

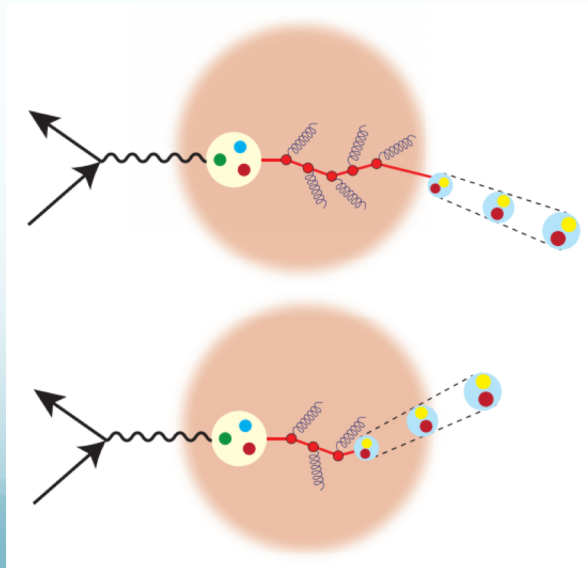


Liu, Moch, Ringer, PRL 2017



# Open questions in e+A DIS

- What is the fundamental quark-gluon structure of light and heavy nuclei?
  - Distribution of quarks and gluons in a nucleus: shadowing, gluon saturation, ...
- Can the nucleus, serving as a color filter, provide novel insights into the propagation, attenuation and hadronization of colored quarks and gluons?
  - Parton propagation, parton energy loss, shower development, ... in the nucleus

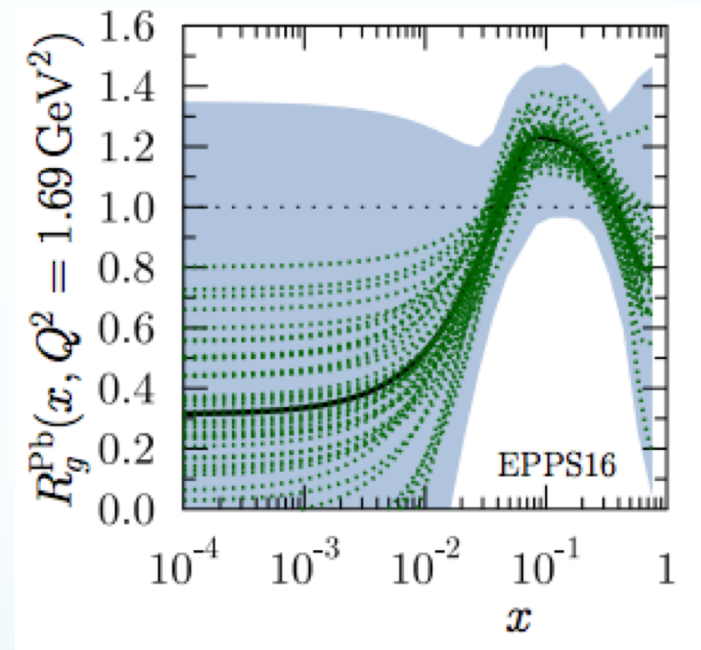
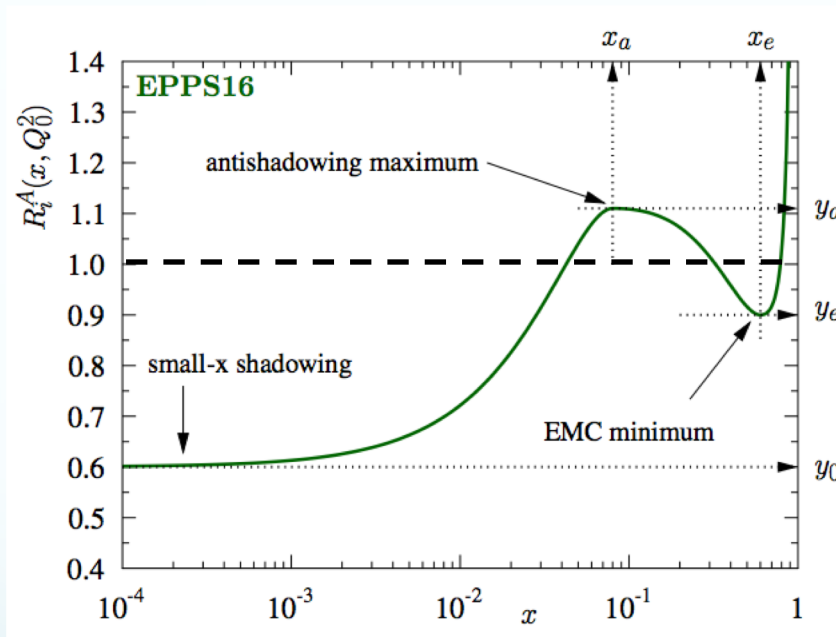


Initial-state effect  
(from modification of PDFs)  
+  
Final-state effect  
(propagation through the nucleus)

# Lesson learned: initial-state effect

- Modification of PDFs in nuclei
  - Very important in describing inclusive DIS data

Eskola, et.al., arXiv: 1612.05471

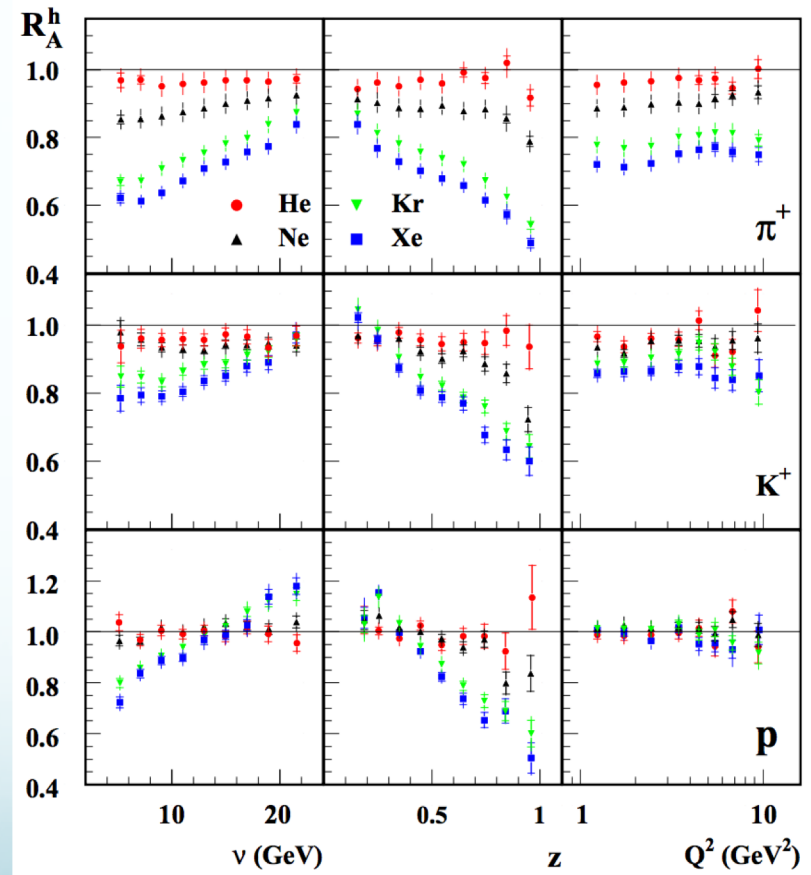


- Of course, small-x effects (color glass condensate) can be studied similarly

# Lesson learned: final-state interaction

- Normalized through inclusive DIS measurements
  - Effects of PDFs in nuclei cancel out in the ratio
  - Modification if there are, must come from final-state interaction in the nucleus

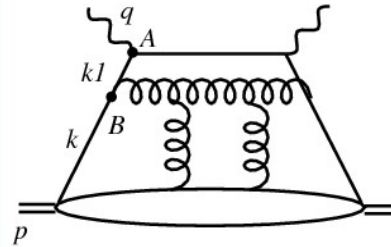
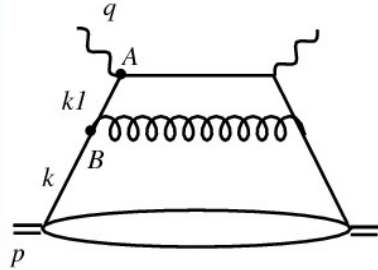
$$R_A^h(\nu, Q^2, z, p_t^2) = \frac{\left( \frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_A}{\left( \frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_D},$$



HERMES, arXiv:0704.3270

# What happens in a large nucleus?

- One method follows from pioneer work of Mueller and Qiu



Nuclear Physics B268 (1986) 427–452  
© North-Holland Publishing Company

## GLUON RECOMBINATION AND SHADOWING AT SMALL VALUES OF $x^*$

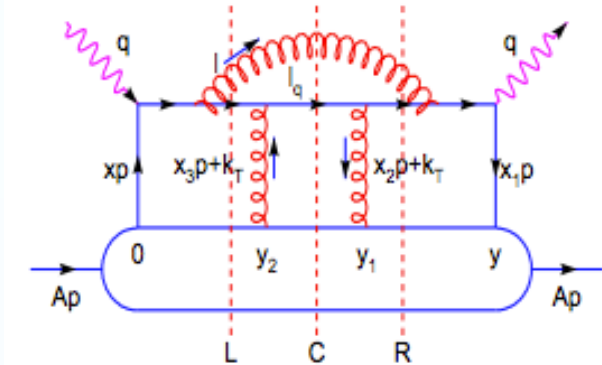
A.H. MUELLER and Jianwei QIU

$$Q^2 \frac{\partial}{\partial Q^2} xG(x, Q^2) = \frac{\alpha C_A}{\pi} \int_x^1 \frac{dx'}{x'} \frac{x}{x'} \gamma^{GG} \left( \frac{x}{x'} \right) x' G(x', Q^2) - \frac{4\pi^3}{N^2 - 1} \left( \frac{\alpha C_A}{\pi} \right)^2 \frac{1}{Q^2} \int_x^1 \frac{dx'}{x'} (x')^2 G^{(2)}(x', Q^2)$$

A power correction term to the usual DGLAP-type evolution

# High-twist approach to jet quenching

- SIDIS as an example: multiple scattering in the medium leads to induced gluon radiation

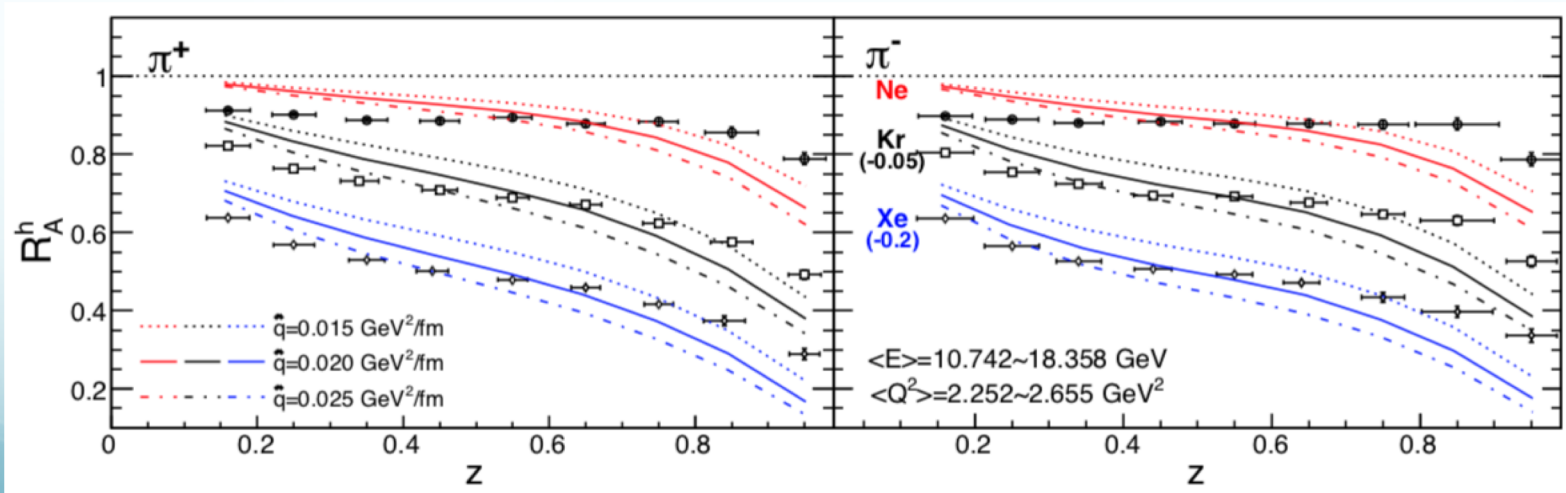


Framework: Qiu, Sterman, 90s

Applications: Wang, Guo, Qin, Majumder, et.al.

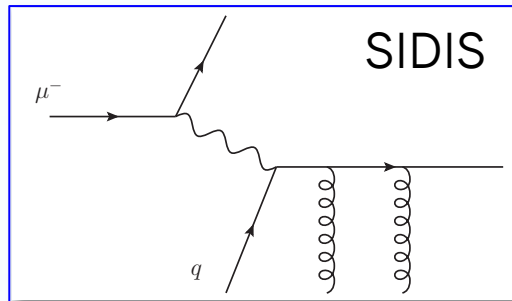
$$\frac{\partial D_i^h(z, \mu)}{\partial \ln \mu^2} = \frac{\alpha_s}{2\pi} [P_{ji}^{\text{vac}} + P_{ji}^{\text{med}}] \otimes D_j^h(z, \mu)$$

- Evolution of fragmentation function is modified Xin-Nian Wang, et.al., 1401.5109

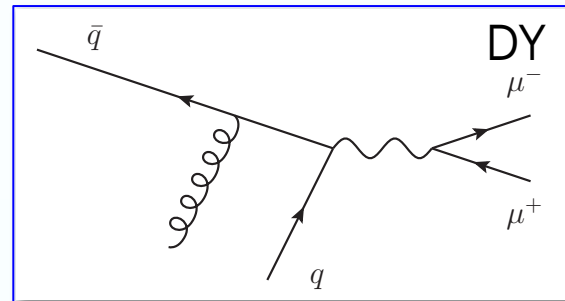


# Parton multiple scattering in the medium

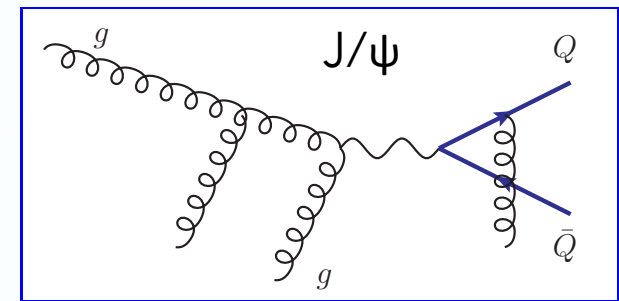
- Transverse momentum broadening (TMB) is sensitive to multiple scattering



$e + A \rightarrow e + h + X$   
Final-state



$p + A \rightarrow \mu^+ \mu^- + X$   
Initial-state

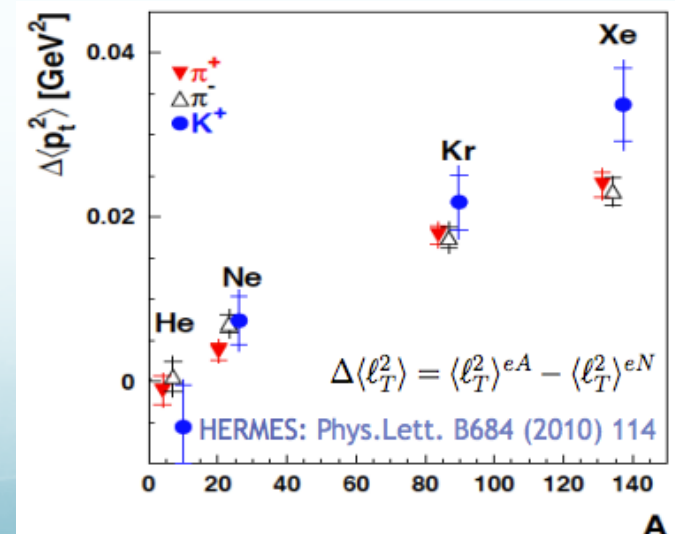


$p + A \rightarrow J/\psi + X$   
Both

- First non-trivial: double scattering

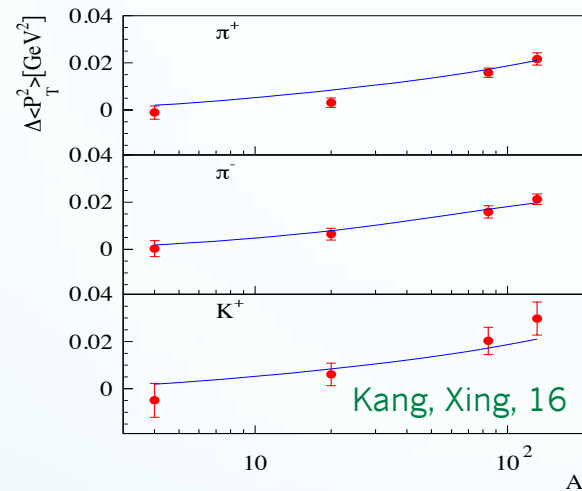
$$\Delta \langle \ell_{hT}^2 \rangle = \langle \ell_{hT}^2 \rangle_{eA} - \langle \ell_{hT}^2 \rangle_{ep}$$

$$\approx \frac{\int d^2 \ell_{hT} \ell_{hT}^2 \frac{d\sigma^D}{dQ^2 d^2 \ell_{hT}}}{\frac{d\sigma}{dQ^2}}$$

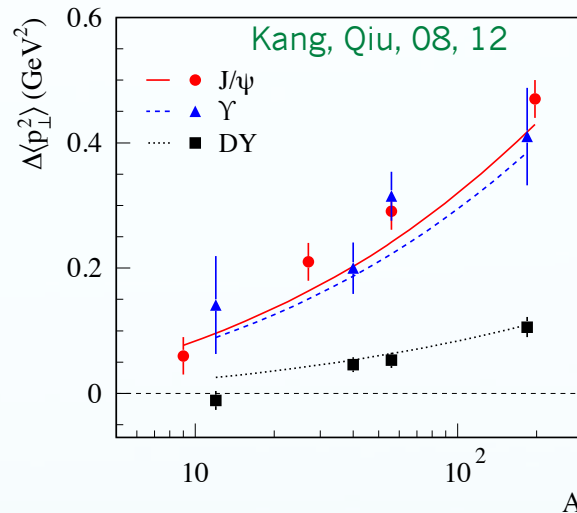


# Works pretty well

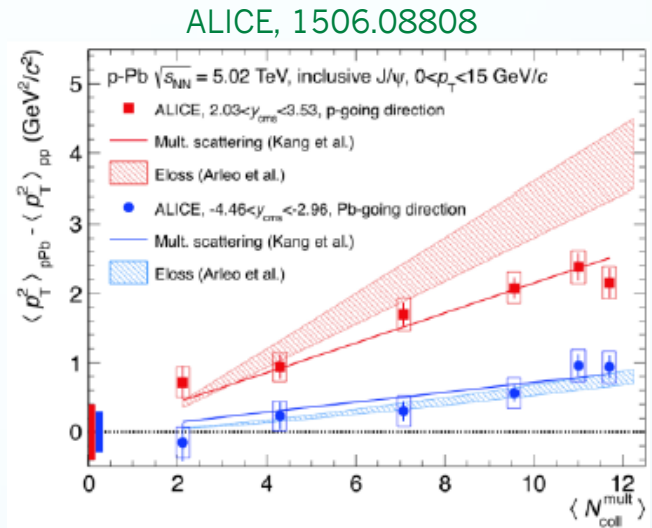
- Description of the data using single set of correlation functions



HERMES



Fermilab, SPS

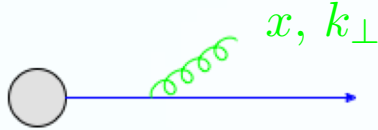


ALICE



# Generalized to hot QCD medium

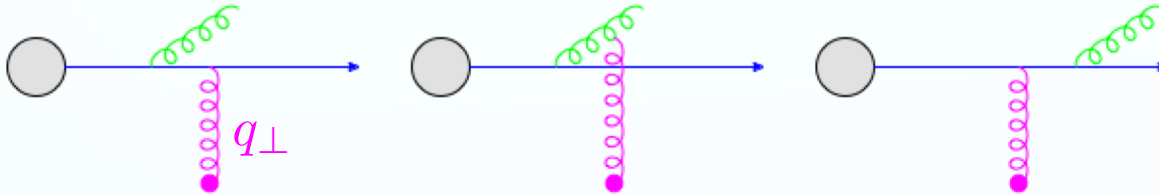
## Vacuum splitting



$$\frac{dN^{\text{vac}}}{dx d^2 k_{\perp}} = \frac{\alpha_s}{2\pi^2} C_F \frac{1 + (1-x)^2}{x} \frac{1}{k_{\perp}^2}$$

## Medium splitting (SCET<sub>G</sub>)

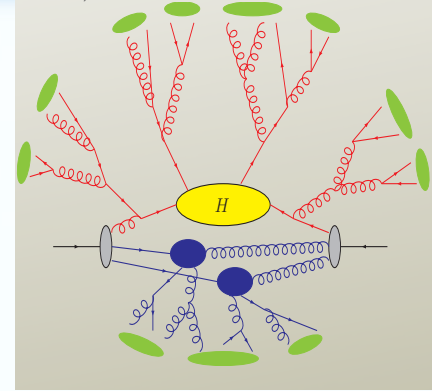
- transverse momentum kick through Glauber gluons  $q \sim (\lambda^2, \lambda^2, \lambda)$



$$\frac{dN^{\text{med}}}{dx d^2 k_{\perp}} = \frac{\alpha_s}{2\pi^2} C_F \frac{1 + (1-x)^2}{x} \int \frac{d\Delta z}{\lambda_g(z)} \int d^2 q_{\perp} \frac{1}{\sigma_{el}} \frac{d\sigma_{el}^{\text{med}}}{d^2 q_{\perp}} \left[ \frac{B_{\perp}}{B_{\perp}^2} \cdot \left( \frac{B_{\perp}}{B_{\perp}^2} - \frac{C_{\perp}}{C_{\perp}^2} \right) (1 - \cos[(\Omega_1 - \Omega_2)\Delta z]) + \dots \right]$$

GLV formalism

Gyulassy, Levai, Vitev, 02, Idilbi, Majumder 08,  
D'Eramo, Liu, Rajagopal, 10, Ovanessian, Vitev, 11, ...

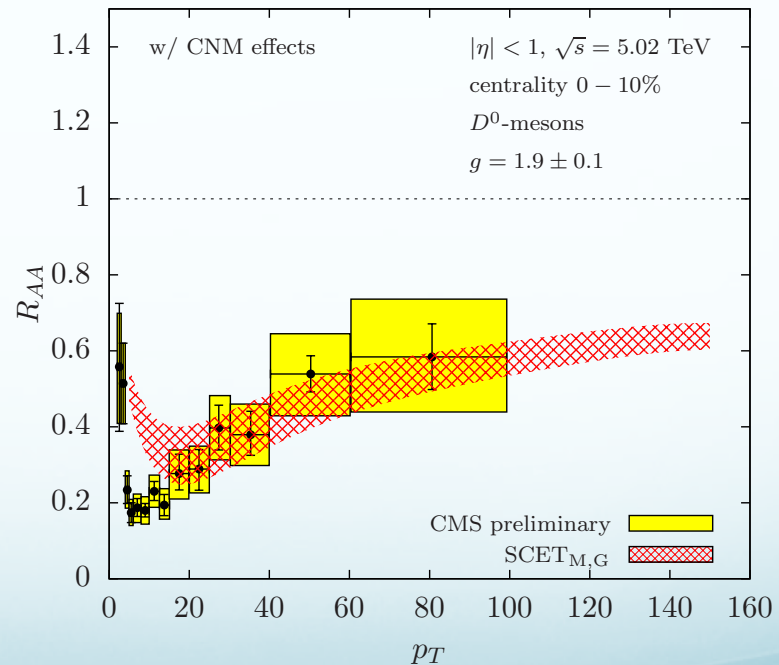
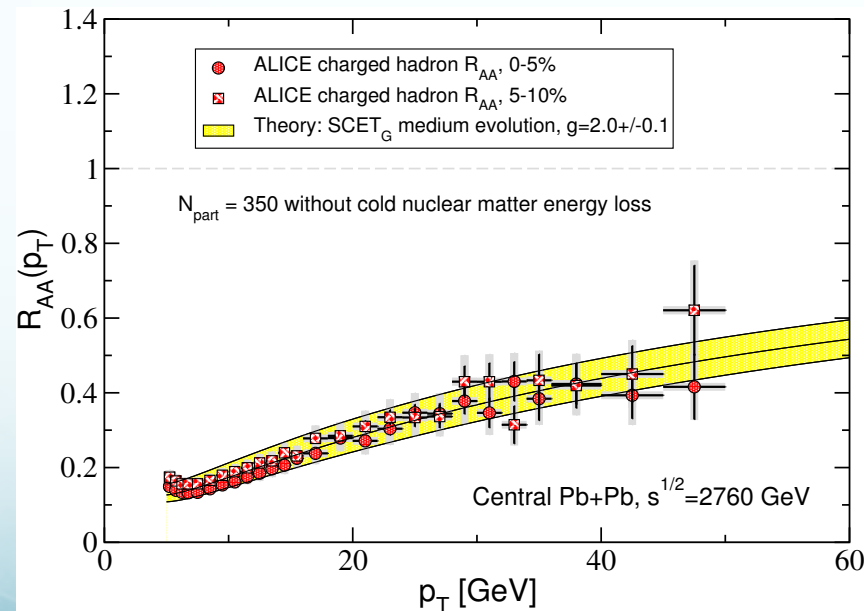




# Light and heavy meson modification

- The fragmentation function modified this way does lead to good description of light and heavy meson in A+A collisions

$$\frac{\partial D_i^h(z, \mu)}{\partial \ln \mu^2} = \frac{\alpha_s}{2\pi} [P_{ji}^{\text{vac}} + \textcolor{red}{P}_{ji}^{\text{med}}] \otimes D_j^h(z, \mu)$$

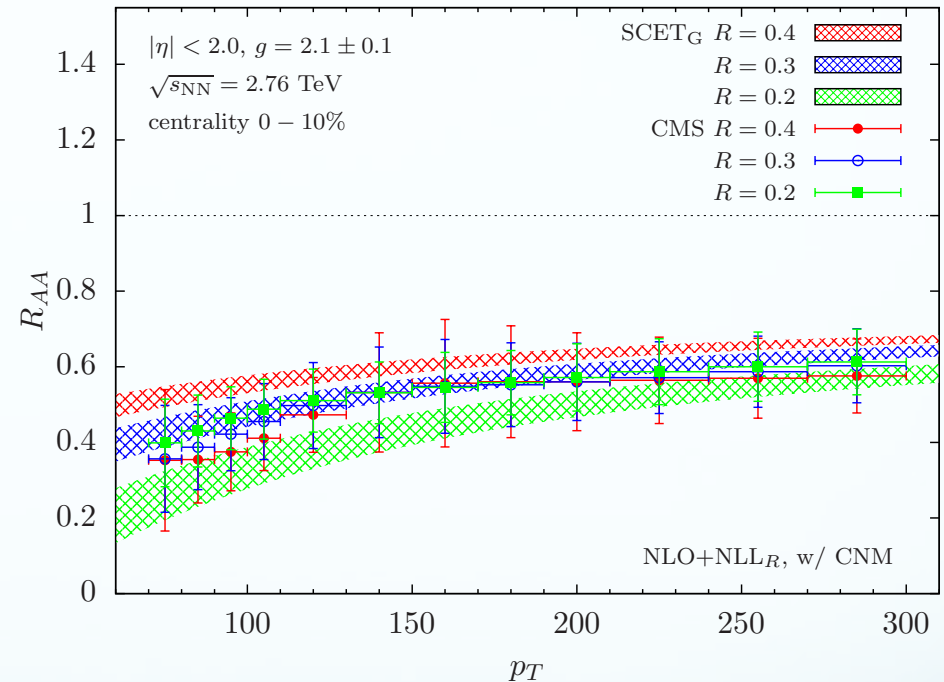
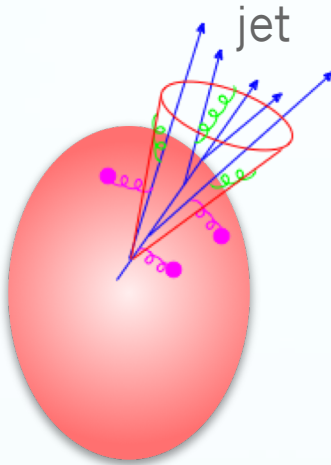


Kang, Ovanesyang, Vitev, et.al., PRL (2015)  
 Chien, Kang, Ovanesyang, Vitev, et.al., PRD (2016)

Kang, Ringer, Vitev, 1610.02043

# Works also for jets

- Inclusive jet cross section also gets modified



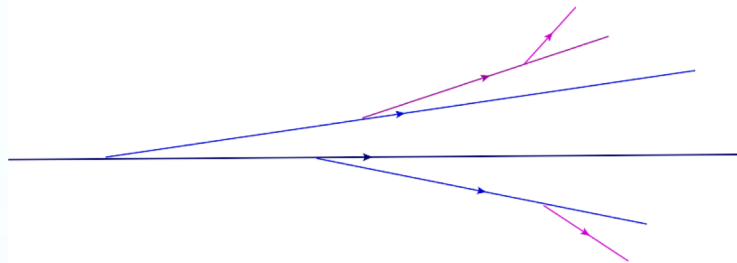
Kang, Ringer, Vitev, 1701.05839

- Expect this framework to be working for
  - Nuclear modification of jet cross section in e+A collisions

# Other thinking of jet evolution in medium

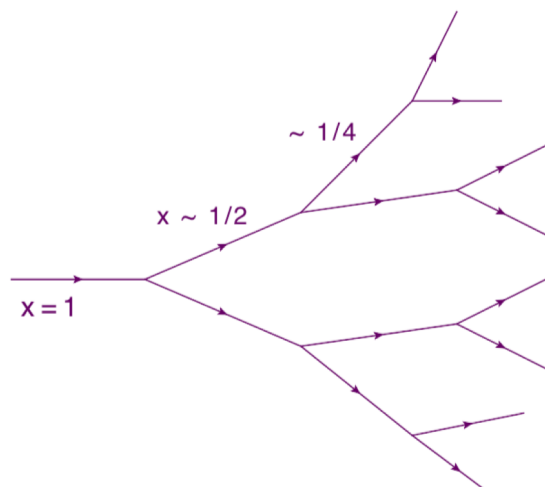
## ■ Vacuum

E. Iancu, hard probe 2015



- quasi-collinear splittings
- pQCD: DGLAP equation
- energy carried by a few partons with large  $x$
- energy remains within a narrow jet

## ■ Medium



- LPM effect  $\Rightarrow$  BDMPSZ emission rate
- multiple, quasi-democratic, branchings
- wave turbulence : highly efficient energy transmission from large  $x$  to small  $x$

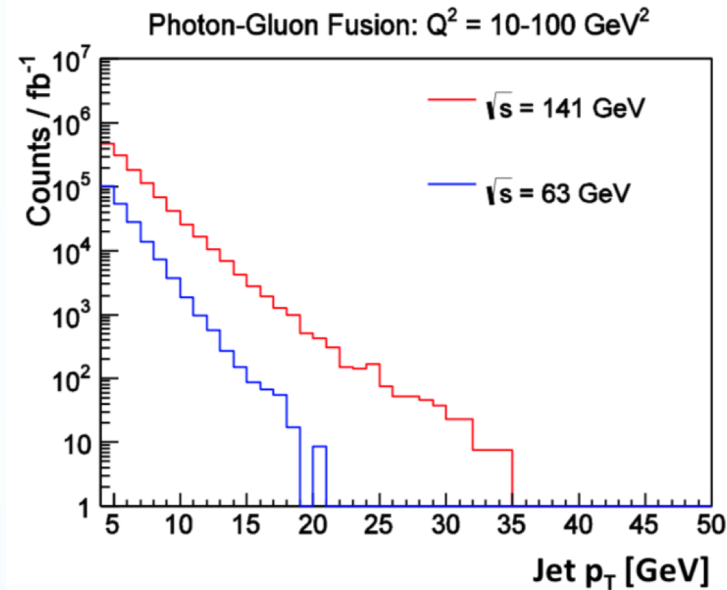
*Blaizot, Dominguez, E.I., Mehtar-Tani (2012...)*

*Apolinário, Armesto, Milhano, Salgado (2014)*

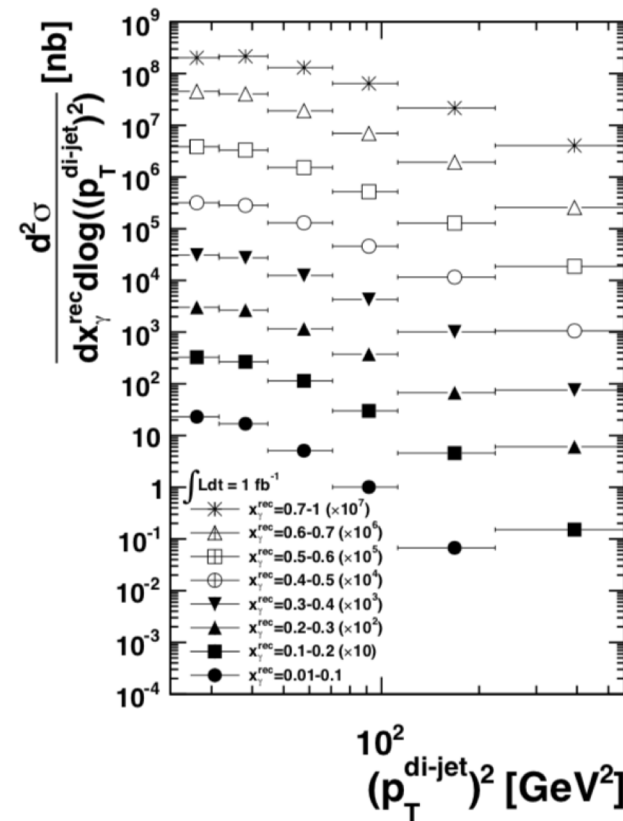
*Kurkela, Wiedemann (2014)*

# Jet physics is promising at EIC

- Plots from EIC team



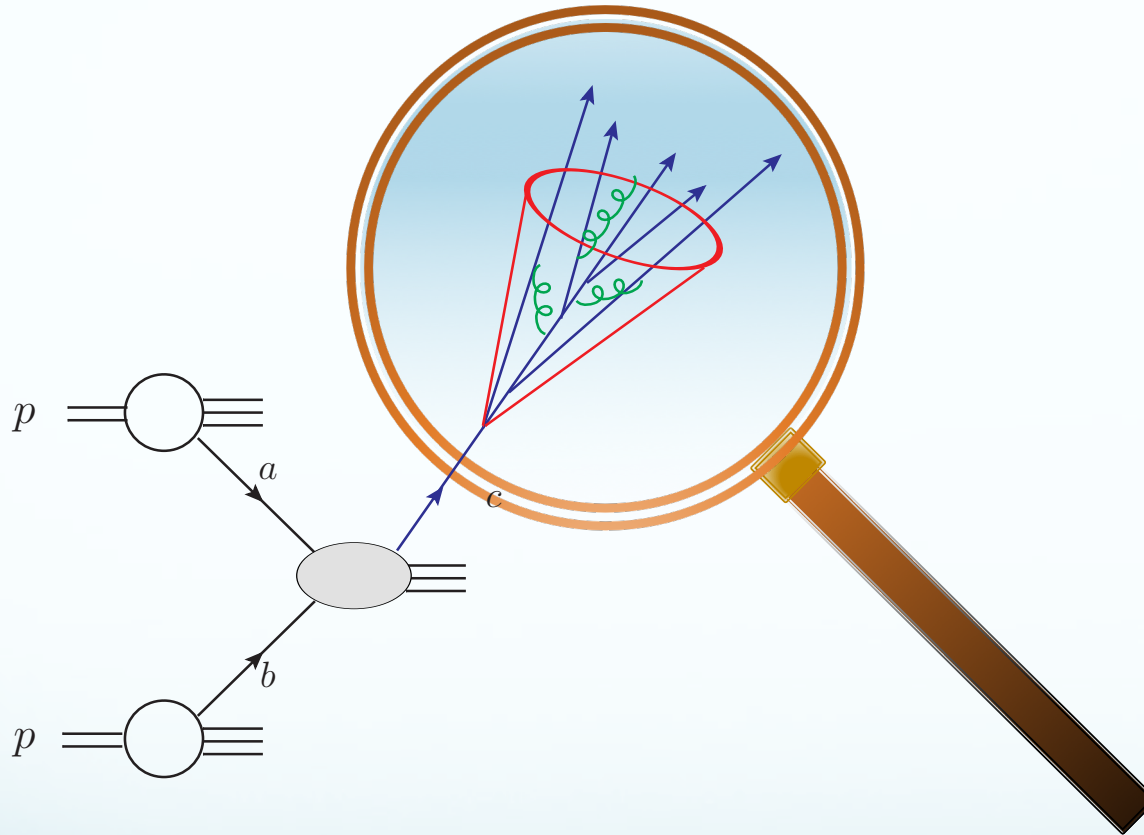
## Photo-production of dijet



See more from B. Page's talk

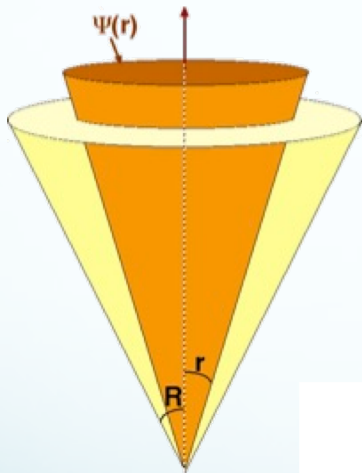
# Jet substructure

- Look inside the jet



# Jet energy profile

- Jet shape: internal energy profile of the jet
- Make sense of the data
  - Quark jet is narrower than gluon jet due to the smaller color charge ( $C_F$  vs  $C_A$ )
  - DIS is dominated by quark jets
  - ppbar is dominated by gluon jets



$$\langle \psi(r) \rangle = \frac{1}{N_{\text{jets}}} \sum_{\text{jets}} \frac{E_T(r)}{E_T^{\text{jet}}}$$

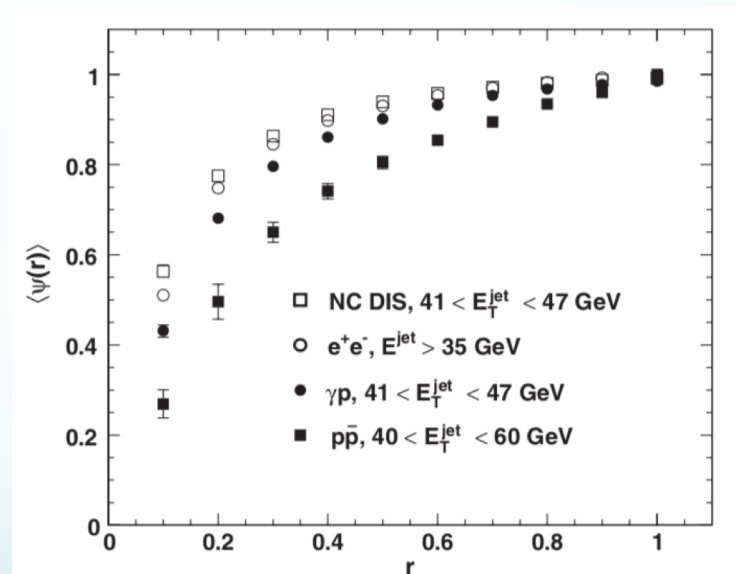
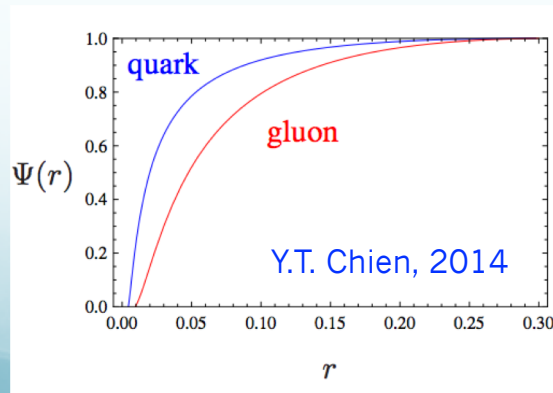


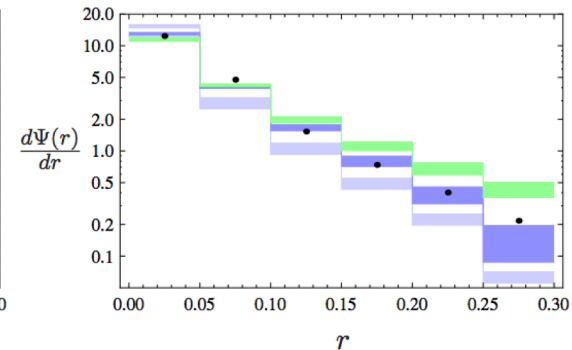
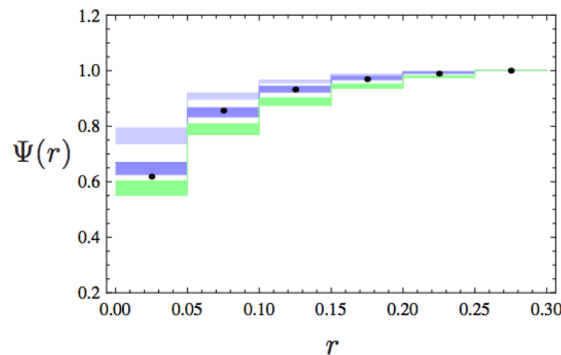
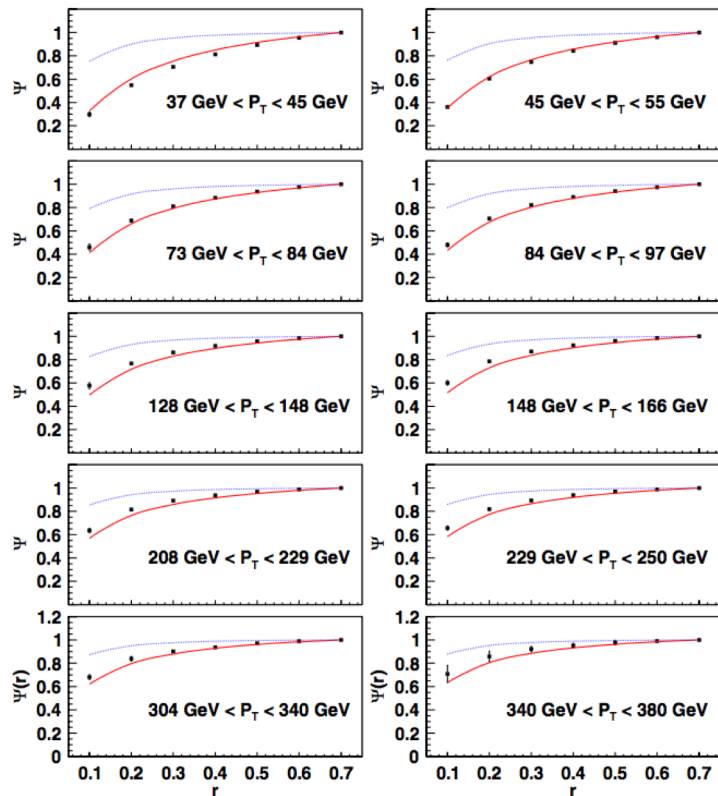
FIG. 13. Measured jet shapes in  $e^+e^-$  scattering (Akers *et al.*, 1994), from ZEUS in DIS (Breitweg *et al.*, 1999c) and photo-production (Breitweg *et al.*, 1998e), and in  $p\bar{p}$  collisions (Abe *et al.*, 1993a; Abachi *et al.*, 1995b). From Butterworth and Wing, 2005.

# Progress since HERA time

- At the time of HERA (pre-LHC), jet substructure is mostly compared with event generators
  - Jet shape: either fixed-order computations or Seymour's MLL results
  - $R \gg r$ : need resummation  $\ln(R/r)$

Compare with jet shape at CDF  
H.n. Li, Z. Li, C.P. Yuan, 2011, 2012

Improved results from Y.T. Chien, I. Vitev, 2014





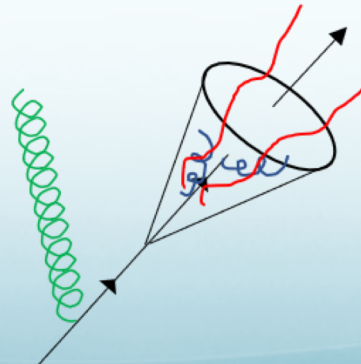
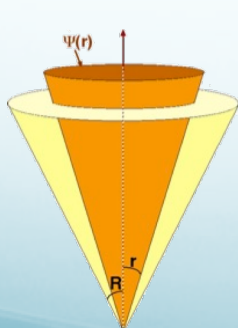
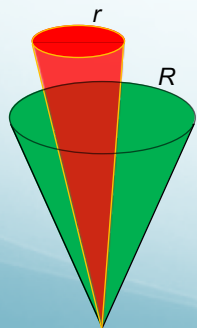
# Further Progress since HERA time

- So far all the theoretical formalism is concentrated only on
  - jet function: only collinear degrees of freedom

$$\Psi(r) = \sum_f \int \frac{dP_T}{P_T} \frac{d\sigma_f}{dP_T} \bar{J}_f^E(1, P_T, \nu_{\text{fi}}^2, R, r) \times \left[ \sum_f \int \frac{dP_T}{P_T} \frac{d\sigma_f}{dP_T} \bar{J}_f^E(1, P_T, \nu_{\text{fi}}^2, R, R) \right]^{-1}$$

- Recently, we find the soft radiation is also important, in order to write down the consistent factorization formalism

$$\hat{\mathcal{G}}_i^{\text{jet}}(z, z_r, \omega_R, r, R, \mu) = H_{ij}(z, \omega_R R, \mu) \int d^2 k_{\perp} C_j(z_r, \omega_r r, k_{\perp}, \mu, \nu) S_j(k_{\perp}, R, \mu, \nu)$$



Kang, Ringer, Waalewijn, 1705.05375

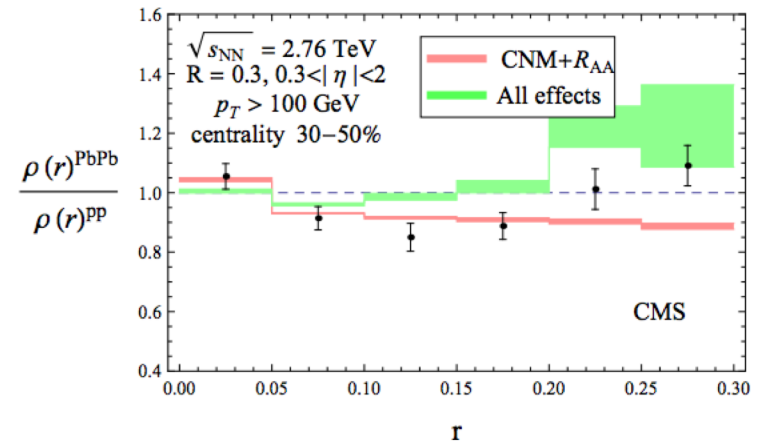
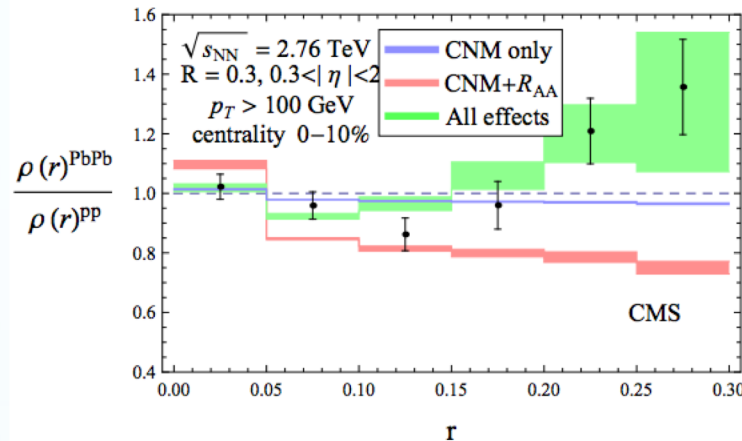
It would be nice to see the phenomenological consequences



# Further Progress in A+A collisions

- Used the same medium-induced splitting functions

Improved results from Y.T. Chien, I. Vitev, 2015

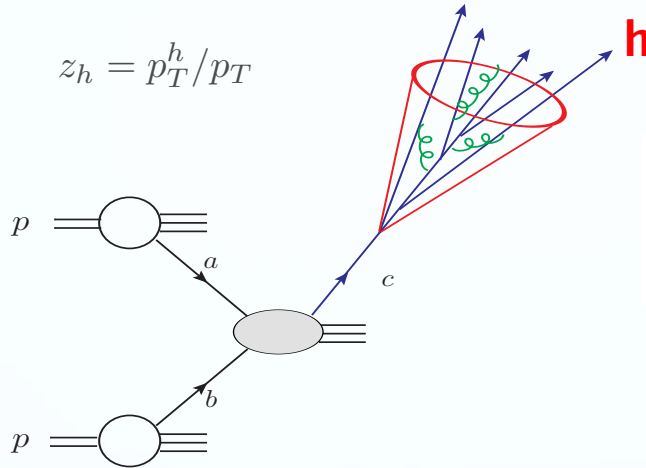


- It would be interesting to make computations for jet shape for both e+p and e+A collisions using new formalism

# Fragmentation inside a jet

- Semi-inclusive fragmenting jet function

Kang, Ringer, Vitev, 1606.07063, JHEP 16



$$\frac{d\sigma^{pp \rightarrow (\text{jet } h) + X}}{d\eta dp_T dz_h} = \sum_{abc} f_a \otimes f_b \otimes H_{ab}^c \otimes \mathcal{G}_c^h$$

- Two DGLAPs: 
$$\mu \frac{d}{d\mu} \mathcal{G}_i^h(z, z_h, \mu) = \frac{\alpha_s(\mu)}{\pi} \sum_j \int_z^1 \frac{dz'}{z'} P_{ji} \left( \frac{z}{z'} \right) \mathcal{G}_j^h(z', z_h, \mu)$$

$$\mathcal{G}_i^h(z, z_h, \mu) = \sum_j \int_{z_h}^1 \frac{dz'_h}{z'_h} \mathcal{J}_{ij}(z, z'_h, \mu) D_j^h \left( \frac{z_h}{z'_h}, \mu \right)$$

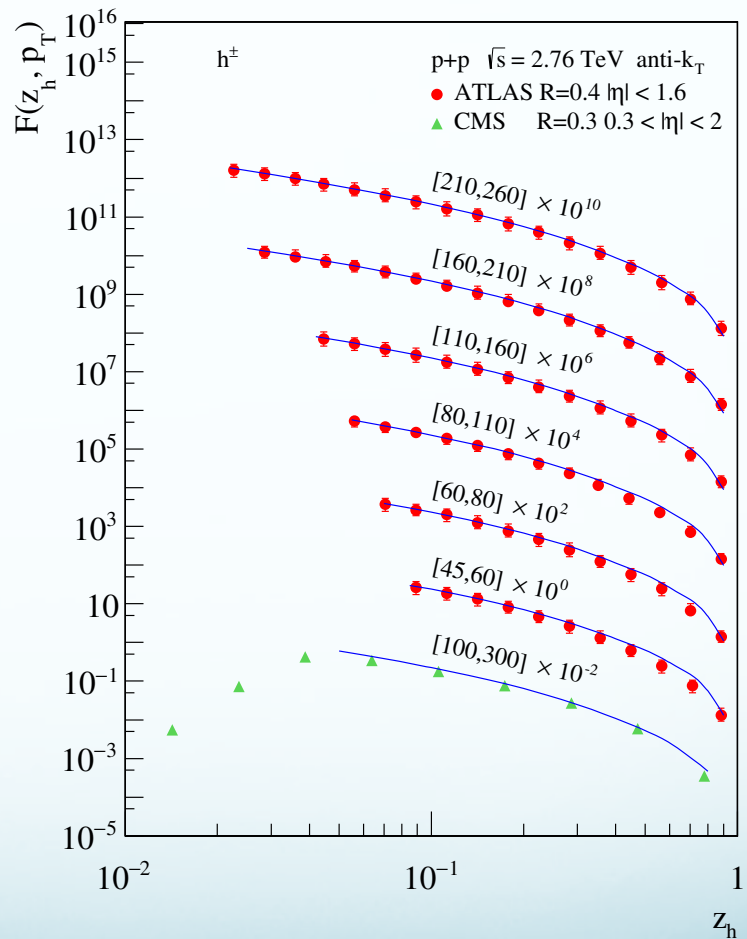
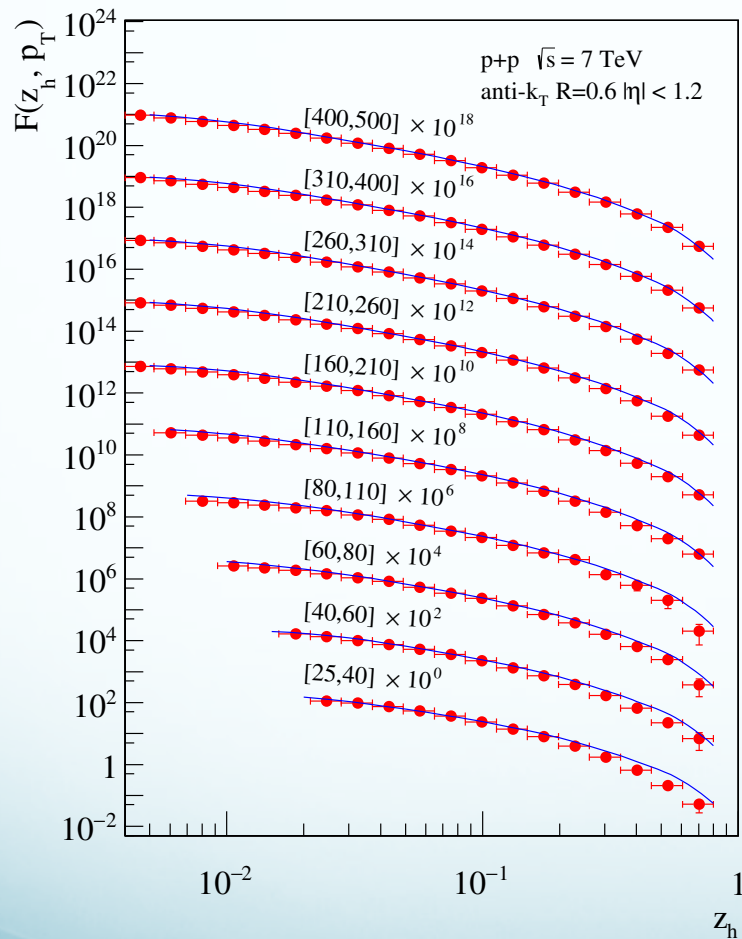
$\mu \sim p_T$

$\mu_J \sim p_T \times R$

$\mu_D \sim 1 \text{ GeV}$

# Light hadrons: work well

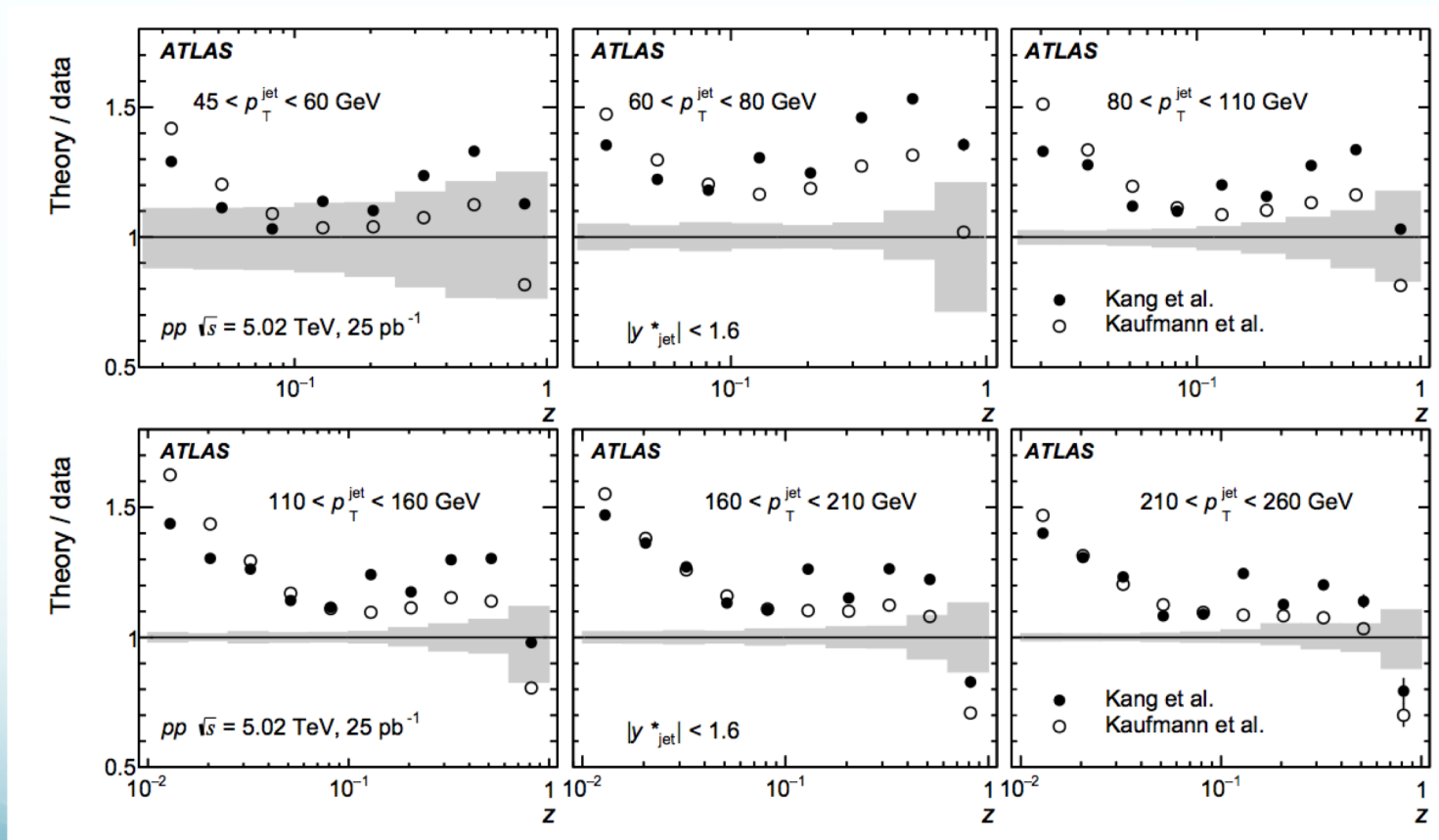
## ■ Light charged hadrons



Kang, Ringer, Vitev, 1606.07063, JHEP, 16

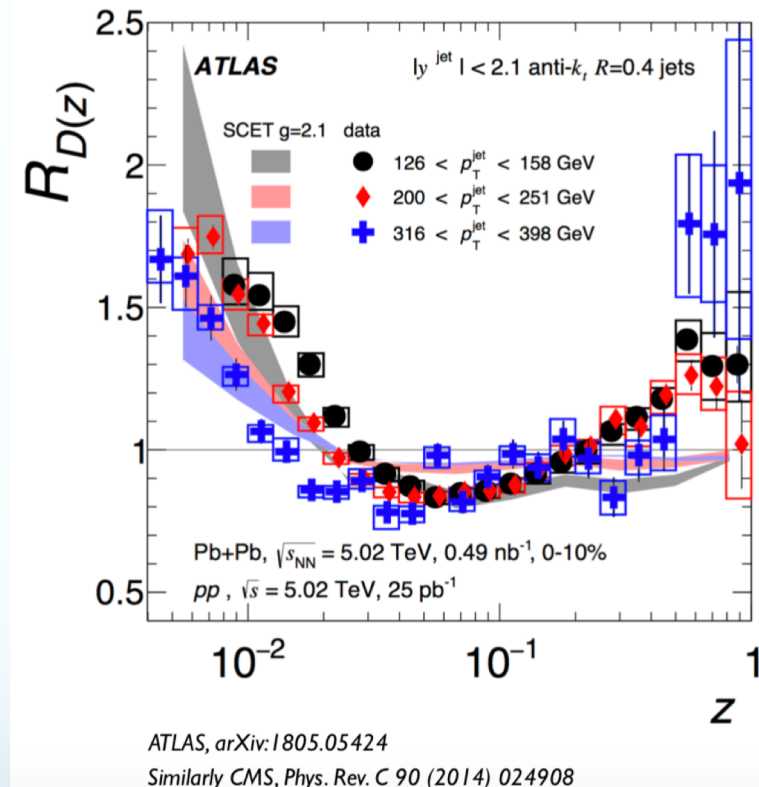
# Further improvement

- So far standard FFs are only constrained for  $z > 0.05$ 
  - These data can constrain small- $z$
  - One might need threshold resummation for large  $z$  region



# Jet fragmentation function in A+A collisions

- Medium modification can be computed similarly once the medium induced splitting functions are given (actual phenomenology is more subtle)



Ringer, CIPANP 2018

- With additional  $R$  in control, should have more power than the usual SIDIS fragmentation functions in e+A collisions

# Jet angularity

- Trust was defined as an event shape parameter to understand radiation pattern

$$T = \frac{1}{Q} \max_{\mathbf{t}} \sum_{i \in X} |\mathbf{t} \cdot \mathbf{p}_i| = 1 - \tau_0$$

- $\tau_0 \rightarrow 0$  is equivalent to dijet limit
- A generalized class of IR safe observables, angularity (applied to jet)

$$\tau_a^{e^+e^-} = \frac{1}{E_J} \sum_{i \in J} E_i \theta_{iJ}^{2-a}$$

$$\tau_a^{pp} = \frac{1}{p_T} \sum_{i \in J} p_{Ti} (\Delta R_{iJ})^{2-a}$$

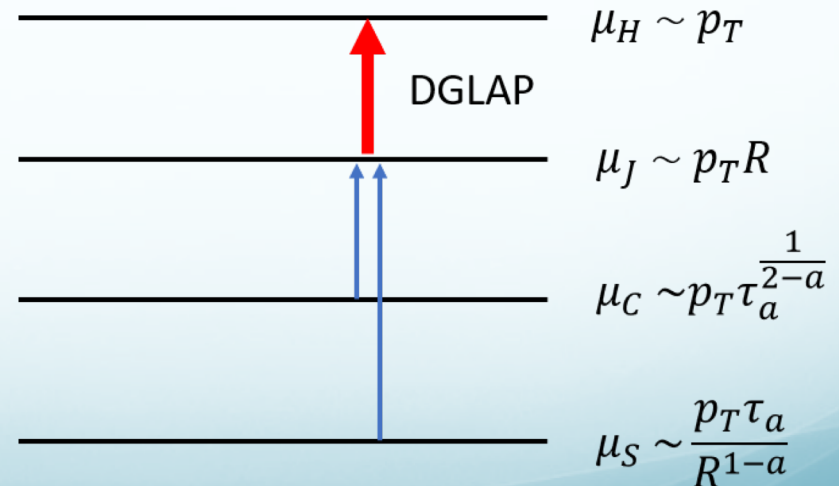
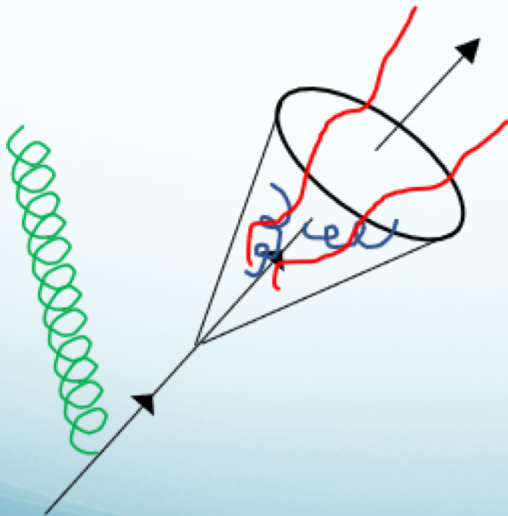
Sterman, et.al. 03, 08, C. Lee, et.al. 10  
Hornig, Makris, Mehen, 16

- $a=0$  related to thrust (jet mass)
- $a=1$  related to jet broadening

# Jet angularity

- Similar replacement:  $J_c(z, p_T R, \mu) \rightarrow \mathcal{G}_c(z, p_T R, \tau_a, \mu)$
- Refactorization

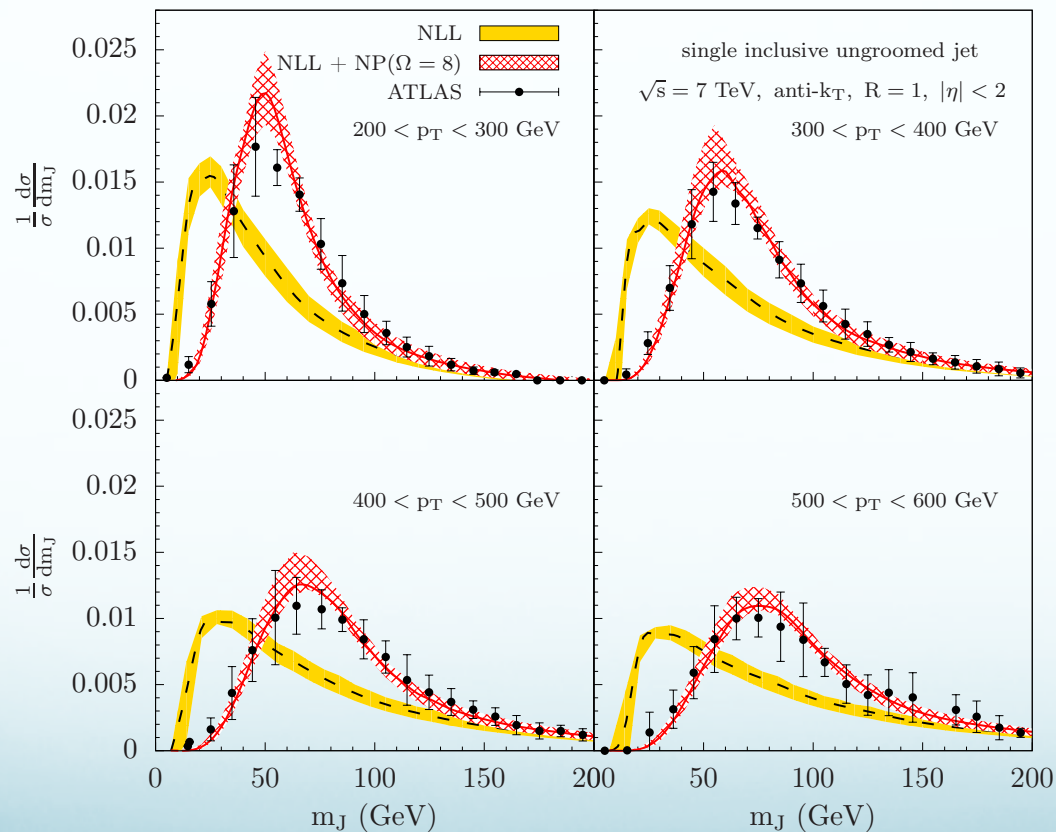
$$\mathcal{G}_c(z, p_T R, \tau_a, \mu) = \sum_i \mathcal{H}_{c \rightarrow i}(z, p_T R, \mu) \times \int d\tau_a^{C_i} d\tau_a^{S_i} \delta(\tau_a - \tau_a^{C_i} - \tau_a^{S_i}) \mathcal{C}_i(\tau_a^{C_i}, p_T \tau_a^{\frac{1}{2-a}}, \mu) \mathcal{S}_i(\tau_a^{S_i}, \frac{p_T \tau_a}{R^{1-a}}, \mu)$$





# Jet mass: $a = 0$

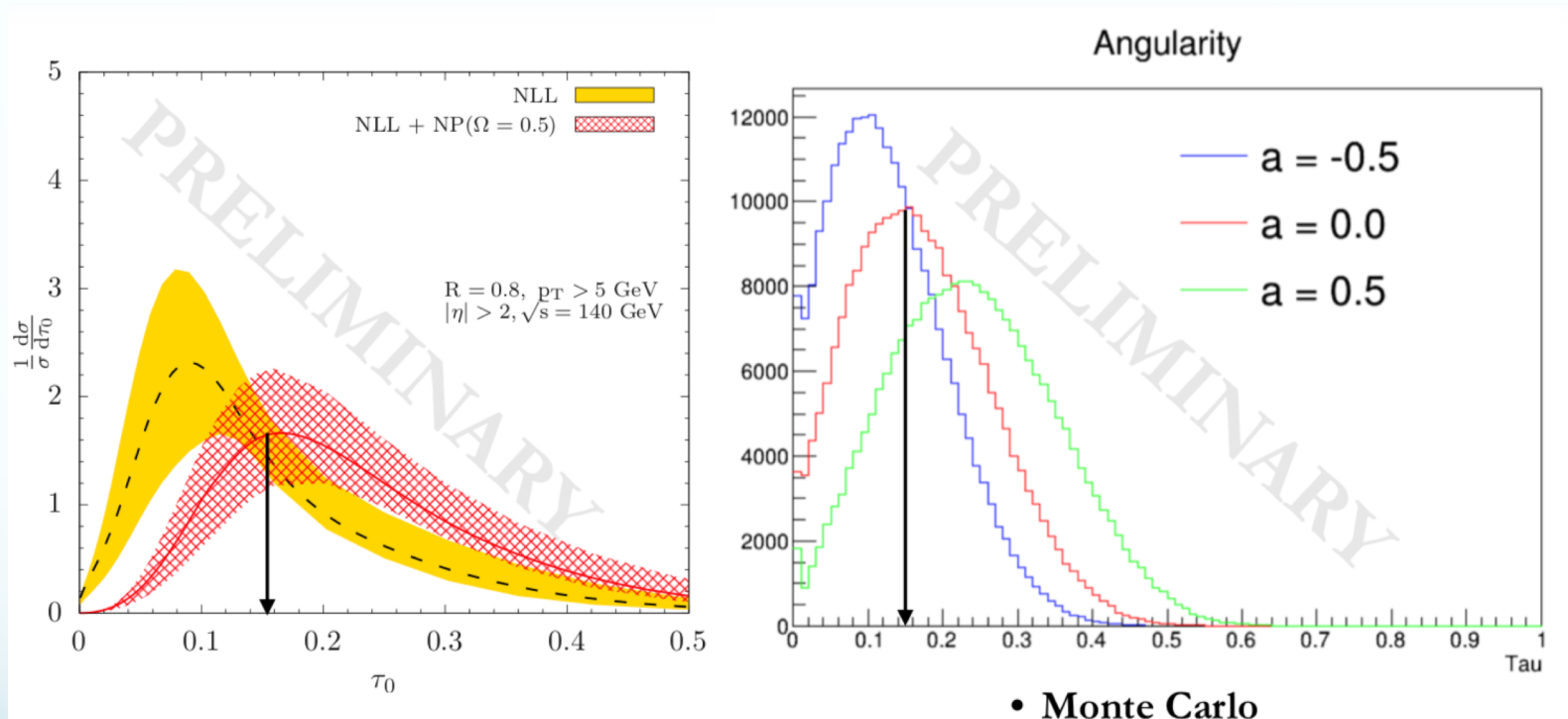
- Comparison with jet mass measurements at the LHC
  - Need a large non-perturbative parameter
  - Strong non-perturbative sensitivity: multi-parton interactions (MPI), pileups, and hadronization (generally need to apply “grooming”, e.g. soft drop grooming)



See details from Kyle Lee's talk

# Jet mass at an EIC

- Computation and comparison with event generator
  - e+A collision is much cleaner environment, likely the main non-perturbative contribution is hadronization effects



Help from B. Page, E. Aschenauer

# Summary

- Even though jet capability at the future EIC is realized only recently, we found that jet physics could be very powerful
  - To understand parton propagation and energy loss in cold QCD matter
  - Especially with the advancement in jet and jet substructure from LHC, the clean environment of e+A collisions should be ideal to constrain the properties of cold QCD matter, probe the underlying mechanism
  - In turn it should lead to better understanding of hot QCD matter
- Exciting jet physics program at EIC

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Thank you!